Comments on "Friis Transmission over a Ground Plane"

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Abstract

The Friis Equation [1] had been used to calculate the power budget between antenna gains and space losses in any radio link with no obstructions in the path between the antenna elements, [10]. It can be used to obtain perfect answers when applied to links in free space and over perfect ground without any modifications or additions.

Index terms—free space the Tx and Rx antennas have the area, gain and factor of the same value [2], [3]. It is important to verify in any radio link if the reciprocity principle is fulfilled, to be:

\[
A eT /g T = A eR /g R = A es /g s
\]

Calculated by a software program (WIPL-D) [6] with the following data,

\[
f = 300 \text{ (MHz)}, \, \theta = 1 \text{ (m)}, \, r = 100 \text{ (m)}, \, R aT = R eR = 71.0 \text{ (?)}, \, R L = 0.0 \text{ (?)}, \, W T = 1 \text{ (W)}.
\]

\[
\begin{align*}
\text{Tx antenna power gain} & = G T = 2.13 \text{ (dBi)}. \\
\text{Tx antenna effective area} & = A eT = 0.13 \text{ (m}^2\text{)}. \\
\text{Rx antenna receiving effective area} & = A eR = 0.0 \text{ (m}^2\text{)}. \\
\text{Rx antenna scattering power gain} & = G s = 2.13 \text{ (dBi)}. \\
\text{Rx antenna scattering effective area} & = A es = 0.13 \text{ (m}^2\text{)}. \\
\text{Rx antenna effective length} & = L eR = 0.3183 \text{ m}. \\
\text{Rx antenna received current} & = I R = 3.1 \times 10^{-4} \text{ (A)}. \\
\text{Rx antenna received voltage} & = V R = 0.0 \text{ (V)}. \\
\text{Rx antenna received power} & = W R = 0.0 \text{ (W)}. \\
\text{Rx antenna scattered power} & = W s = 6.91 \times 10^{-6} \text{ (W)}.
\end{align*}
\]

In his original book "ANTENNAS" Dr. John Kraus [2] took as scattering area A es the relation between the reradiated or scattered power W s and the incoming power density P i instead of calculating the scattering area A es , that was suggested by Harald Friis [3], for the case of a transmitting or retransmitting antennas, according to the radiated numerical gain g T or scattered numerical gain g s . This event was repeated incorrectly in several other antenna theory books. Using the scattered area by Dr. Kraus the scattered gain G s would acquire more than 8 (dBi) which is not possible for a simple half-wave dipole antenna in short circuit and free space. It can show calculations, that the maximum gain in short circuit, is exactly \( G s = 2.15 \text{ (dBi)} \) like the Tx antenna [10].

In reality both antennas are doing practically the same task, the Tx fed by the theoretical generator with zero internal impedance and the Rx fed by the incoming wave. This can be verified simply by means of the current distribution of both antennas fed by the same voltage \( V T = V i \) where \( V i = E i * L eR \). \( E i \) is the electrical field intensity of the incoming wave and \( L eR \) is the antenna effective length. Figure 1 shows the same results as the Figure 3 in page 47 of Dr. Kraus antenna book [2], where the maximum effective scattering and receiving areas have the same value. Possibly in the fifties the most important task of a radio link was the radio communication for telegraphic or telephonic applications. Presently, electronic warfare and radar requires the knowledge of EM scattering of the Rx antennas in free space or installed over ground. The truth is in favor of Schelkunoff and Friis [3], because in their book the main Friis equation utilizing the main antenna parameters, Calculated by a software program (WIPL-D) [6] with the following data,

\[
\begin{align*}
\text{Tx antenna power gain} & = G T = 2.15 \text{ (dBi)} \text{ over perfect ground } [2], [3] . \\
\text{G T} & = 2.15 \text{ (dB)(free space)} + 3 \text{ (dB)(image effect)} + 3 \text{ (dB)(half sphere space radiation)} = 8.15 \text{ (dB)} \text{ (6 dB gain of the same antenna in free space)}.
\end{align*}
\]

\[
\text{Rx antenna effective receiving area} = W R /P i A eR = 0.079 \text{ A eR} /g R = 0.079
\]

\[
A eR /g s = 0.079
\]

\[
\text{Power reciprocity principle fulfilled. Incident power density or Poynting vector: } P iM = (RP 2 y + RP 2 z )
\]

\[
1/2 = 5.139E ? 5(W/m 2 ).
\]

\[
\text{Power density elevation angle of the Tx radiation pattern first lobe: } \theta M = \tan ^{-1}(RP z /RP y ) = 7.2 ^{?}.
\]

\[
\text{Of course, exactly the same elevation angle of the Tx antenna radiation pattern. The maximum power density } P iM \text{ is travelling along the line of distance } r' \text{ between antennas shown in Figure 2 and at the lower lobe shown in figure 3, fulfilling the Fermat principle. Maximum scattering power density } P sM \text{ has an elevation angle for}
\]
the first lobe of ? sM = 1.1 ? due to the Rx antenna scattering radiation pattern at the height H R . The Rx antenna is a more complex system than the Tx antenna because it needs to deliver power to the load R L and, at the same time, scatters EM energy to the surrounding space. These two tasks have a different radiation patterns, as suggested by Schelkunoff and Friis [3] in his antenna book, but this property was not expanded in their treatise. Rx antenna pattern is practically omnidirectional because it delivers the EM energy on its resistive load but nothing on its image, so it is performing like in free space. This is confirmed by its gain of around 2 (dBi) and almost constant if the Rx antenna is scanned in its height H R [7]. In this case the G R is always close to 2 (dBi) from H R till very close to ground and decreasing slowly to ??(dBi) at zero height. The Rx antenna scattering pattern depends, like a Tx antenna, on its height over ground as shown in Figure [3]. In this case the Rx antenna height is 12.6 ? and it produces 25 lobes between zero and 90 degrees. The Tx antenna at 2 ? height produces 4 lobes as shown in Figure [3]. It is useful to see the area, gain and factor relation between the Tx and Rx antennas working over perfect ground:

\[
\frac{A eT}{A eR} = 0.52/0.13 = 4.0 \ (6 \, \text{dB}) \quad \text{g T/g R} = 6.56/1.65 = 3.98 \ (6 \, \text{dB}) \quad \text{Af T50/AF R50} = 3.80/7.58 = 0.5 \ (76 \, \text{dB})
\]

For identical resonant and perfectly matched antennas over perfect ground the difference between Tx and Rx antennas of area, gain and factor is 6 dB [10].

Following values are considered: \( f = 300 \, \text{(MHz)} \), ? = 1 (m), r = 100 (m), H = 0.236 (m). IV. Rx Antenna in Short Circuit over Perfect Ground Yielding these results by software program (WIPL-D) [6], or:

\[
\text{Tx antenna power gain } G T = 8.18 \, \text{(dBi)} \\
\text{Tx antenna effective area } A eT = 0.52 \, \text{(m}^2) \\
\text{Rx antenna receiving effective area } A eR = 0.065 \, \text{(m}^2) \\
\text{Rx antenna theoretical power gain } G R = 0.26 \, \text{(dBi)} \\
\text{Rx antenna theoretical effective area } A eR = 0.06 \, \text{(m}^2) \\
\text{Rx antenna theoretical receiving power gain } G s = 2.15 \, \text{(dBi)} \\
\text{Rx antenna theoretical receiving effective area } A es = 0.13 \, \text{(m}^2) \\
\text{Rx antenna effective receiving area } A eR = 0.13 \, \text{(m}^2)
\]

In this case, Tx and Rx antenna have practically the same maximum power gain but different amount of lobes depending on their height over ground. Also, the effective scattering area calculated by the scattering numerical gain g s or by the relation between the scattered power W s and the incoming power density P i yields practically the same result [10].

\[
\text{Tx antenna theoretical power gain } G T = 5.15 \, \text{(dBi)} \\
\text{Tx antenna theoretical effective area } A eT = 0.26 \, \text{(m}^2) \\
\text{Rx antenna theoretical power gain } G R = 0.159 \, \text{(dBi)} \\
\text{Rx antenna theoretical effective area } A eR = 0.066 \, \text{(m}^2) \\
\text{Rx antenna theoretical receiving power gain } G s = 2.15 \, \text{(dBi)} \\
\text{Rx antenna theoretical receiving effective area } A es = 0.13 \, \text{(m}^2) \\
\text{Rx antenna theoretical effective receiving area } A eR = 0.13 \, \text{(m}^2)
\]

V. Radio Link between Two Identical Quarter-Wave Monopole Antennas over Perfect Ground "A radio link between two half-wave dipole antennas in free space delivers the same power W R in the receiving load as a radio link between two quarter wave monopole antennas over perfect ground if the power W T and distance r is the same, or:

\[
\text{Relations are very close to } 6 \, \text{dB} [10]. \text{ The power received } W R = 1.68E^{-6} \, \text{(W)} \text{ by this radio link is exactly the same as the radio link between two identical half-wave dipole antennas in free space shown previously. This fulfills the Kenneth Alva Norton Statement [4], or:}
\]

\[
\text{V. Radio Link between Two Identical Quarter-Wave Monopole Antennas over Perfect Ground "A radio link between two half-wave dipole antennas in free space delivers the same power W R in the receiving load as a radio link between two quarter wave monopole antennas over perfect ground if the power W T and distance r is the same, or:}
\]

\[
\text{Calculations performed here show that the Norton Statement [4] is perfectly fulfilled if the real or natural antenna gains are used and, therefore, no artificial factors are needed to be introduced to fulfill this Statement, as well as the Friis power budget and the power reciprocity principle [7,8].}
\]

Here no antenna gain were changed in any case like in the papers commented, [7], [8], to force the power budget fulfillment.

\[
\text{Tx antenna theoretical power gain } G T = 5.15 \, \text{(dBi)} \\
\text{Tx antenna theoretical effective area } A eT = 0.26 \, \text{(m}^2) \\
\text{Rx antenna theoretical effective height } H eT = 0.318 \, \text{(m)} \\
\text{Rx antenna theoretical receiving effective area } A eR = 0.065 \, \text{(m}^2) \\
\text{Rx antenna theoretical receiving power gain } G s = 2.15 \, \text{(dBi)} \\
\text{Rx antenna theoretical effective area } A es = 0.13 \, \text{(m}^2)
\]

1 Schelkunoff and Friis power reciprocity principle [3]:

\[
\text{A eT/g T} = 7.96E^{-6} \, ? 2 \quad \text{A eR/g R} = 7.96E^{-6} \, ? 2 \quad \text{A es/g s} = 7.96E^{-6} \, ? 2
\]

Power reciprocity principle fulfilled. Monopole antennas, factor, area and gain relations are obtained, as: aF

\[
\text{Af T50/AF R50} = 5.40/10.68 = 0.51 \, (?5.92dB)
\]

\[
\text{A eT/A eR} = 0.26/0.066 = 3.94 \, (5.95dB)
\]

\[
\text{g T/g R} = 3.25/0.83 = 3.92 \, (5.93dB)
\]

\[
\text{Relations are very close to } 6 \, \text{dB} [10]. \text{ The power received } W R = 1.68E^{-6} \, \text{(W)} \text{ by this radio link is exactly the same as the radio link between two identical half-wave dipole antennas in free space shown previously. This fulfills the Kenneth Alva Norton Statement [4], or:}
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\[
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\]

\[
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\]

\[
\text{Tx antenna theoretical power gain } G T = 5.15 \, \text{(dBi)} \\
\text{Tx antenna theoretical effective area } A eT = 0.26 \, ? 2 \\
\text{Rx antenna theoretical effective height } H eT = 0.318 \, ? 2 \\
\text{Rx antenna theoretical receiving effective area } A eR = 0.065 \, ? 2 \\
\text{Rx antenna theoretical scattering power gain } G s = 2.15 \, (dBi) \\
\text{Rx antenna theoretical scattering effective area } A es = 0.13 \, ? 2 \\
\text{Rx antenna theoretical effective height } H eR = 0.13 \, ? 2
\]
2 Results using software program (WIPL-D) [6]:

The voltage \( V \) on the radiation resistance \( R_\text{aT} \), results in:

\[
V_T = (I_T R_{\text{aT}}) = 0.6455 \times 0.24 = 0.155 \text{ (V)}
\]

Transmitted power \( W_T \) depends from the radiation resistance \( R_{\text{aT}} \) and the squared current \( I_T^2 \) of the transmitting antenna. This way, the voltage \( V_g \) from the generator or amplifier must be:

\[
V_g = (V_Rg + V_Z_{\text{aT}}) = 1431 + 32.3 = 1463.3 \text{ (V)}
\]

The voltage \( V_Rg = 50 \text{ (?)} \) on the generator or amplifier impedance, in order to feed the transmitting antenna, results in:

\[
V_T = (I_T R_{\text{aT}}) = 0.6455 \times 0.24 = 0.155 \text{ (V)}
\]

Transmitted power \( W_T \) depends from the radiation resistance \( R_{\text{aT}} \) and the squared current \( I_T^2 \) of the transmitting antenna. This way, the voltage \( V_g \) from the generator or amplifier must be:

\[
V_g = (V_Rg + V_Z_{\text{aT}}) = 1431 + 32.3 = 1463.3 \text{ (V)}
\]

The voltage \( V_Z_{\text{aT}} \) is obtained by a WIPL-D software [6], or:

\[
Z_{\text{aT}} = (R_{\text{aT}} + jX_{\text{aT}}) = (0.24 - j2217) \text{ (?)}
\]

In decibels, results in:

\[
\text{AF}_{50} = 20 \log E_i V_{50} \text{ (dB/m)}
\]

For a short monopole antenna \( H_R \geq 0.1 \), its effective height \( H_{eR} \) when the wave impedance is \( Z_w = Z_{00} \) is:

\[
H_{eR} = 0.12 \times 377 \times !
\]

Where: \( V_i \) (V/m) is the induced voltage by the incoming wave in the Thevenin receiving antenna equivalent circuit. \( E_i \) (V/m) is the incoming electric field on the receiving monopole antenna.

3 VI. Rx Quarter-Wave Monopole

Antenna in Short Circuit Thus: \( E = V = i H eR \) (V /m)(4)

From this relation NIST determines the receiving antenna factor \( a_F \) in the 50 ? calibrated receiver, or:

\[
a_F = \frac{R_{50}}{E = i V R50} = \frac{V R50}{R_50} \text{ (dB/m)}(2)
\]

I R y R L50 are common factors in numerator and denominator, results in:

\[
a_F \approx 1 + Z_{\text{R}} R_{L50} H_{eR}
\]

If \( L50 = 50 \text{ (?)} \) the NIST receiving antenna factor equation, is:

\[
a_F = X_{\text{R}} R_{50} H_{eR} = X_{\text{R}} R_{25} H_{eR}
\]

In decibels, results in:

\[
\text{AF}_{50} = 20 \log X_{\text{R}} \text{ (dB/m)}(9)
\]

NIST doesn’t determine the receiving antenna input impedance but the receiving antenna capacity using the well known antenna capacity by the equation published by Schelkunoff and Friis [3], or:

\[
C_{\text{aR}} = 2 \times 0.1 H \ln(H/a)
\]

From this equation the capacitive reactance \( X_{\text{aR}} \) is obtained:

\[
X_{\text{aR}} = 120 \times 377 \times !
\]

Where: \( V_i \) (V) is the induced voltage by the incoming wave in the Thevenin receiving antenna equivalent circuit.

\[
E_i \text{ (V/m)}
\]

4 Using this procedure, where \( R_{\text{aR}} \) is negligible, the receiving antenna factor \( a_F \) is reactive and practically imaginary. Here, the simulation is performed as an example at the frequency \( f = 3 \text{ (M Hz)} \) by means for a radio link between two monopole antennas with the same physical geometry like NIST. The input impedance of both monopoles is obtained by a WIPL-D software [6], or:

\[
Z_a = (R_a + jX_a) = (0.24 - j2367) \text{ (?)}(13)
\]

Transmitted power \( W_T \) depends from the radiation resistance \( R_{\text{aT}} \) and the squared current \( I_{\text{2T}} \) of the transmitting antenna and for a transmitted power \( W_T = 0.1 \text{ (W)} \), results in:

\[
I_{\text{T}} = W_T R_{\text{aT}} \times 0.12 = 0.1 \times 0.24 = 0.06455 \text{ (A)}(14)
\]

The voltage \( V_T \) on the radiation resistance \( R_{\text{aT}} \), results in:

\[
V_T = (I_T R_{\text{aT}}) = 0.6455 \times 0.24 = 0.155 \text{ (V)}
\]

The voltage \( V_a = V_T \) on the transmitting antenna impedance \( Z_{\text{aT}} \), results in:

\[
V_a = (I_T Z_{\text{aT}}) = (V Z_{\text{aT}}) \text{ (V)}(16)
\]

The voltage is complex with the real part very small compared to the imaginary part. Its module is obtained as:

\[
|V Z_{\text{aT}}| = 1431 \text{ (V)}(18)
\]

The voltage \( V_R \) is obtained on the generator or amplifier impedance, in order to feed the transmitting antenna, results in:

\[
V_R = (I_T R_{\text{g}}) = 0.6455 \times 0.24 = 0.155 \text{ (V)}
\]

This way, the voltage \( V \) from the generator or amplifier must be:

\[
V = (V_R + V_a) = 1431 + 32.3 = 1463.3 \text{ (V)}(20)
\]
The necessary power $W_g$ to produce the transmitting power $W_T = 0.1$ (W), result in:

$$W_g = (V_g I_T) = 1463.3 \times 0.6455 = 944.56$$ (W) \hspace{1em} (21)

It is very important to see the low efficiency of the power supply when a transmitting antenna is very reactive and with no impedance matching. Almost 1 KW to radiate 100 mW. For this reason NIST uses a power amplifier to feed the transmitting short monopole. But it is the only way to feed a wide band short antenna at frequencies lower than 10 MHz. In simulation the voltage using WIPL-D to feed the transmitting antenna is $| V Z a T | = 1431$ (V) and transmitting gain, field strength and power density obtained at the distance $r = 30$ (m), are:

$$G_T = 4.$$ \hspace{1em} (22)

Thus:

$$E_i = V_i H eR (V/m) \hspace{1em} (4)$$

From this relation NIST determines the receiving antenna factor $a F R 50$ in the 50 ? calibrated receiver, or:

$$a F R 50 = E_i V R 50 = V_i V R 50 H eR = I R (R L 50 + Z a R ) I R R 50 H eR = (1/m) \hspace{1em} (5)$$

$I R$ and $R 50$ are common factors in numerator and denominator, results in:

$$a F R 50 = 1 + Z a R R 50 H eR \hspace{1em} (1/m) \hspace{1em} (6)$$

$Z a R = R aR + j X aR$ is input impedance of the receiving antenna where the imaginary part $X aR$ is greater than the real part $R aR$ or:

$$Z a R = R aR + j X aR \hspace{1em} (?) \hspace{1em} (7)$$

With $R 50 = 50$ (?) the NIST receiving antenna factor equation, is:

$$a F R 50 = X aR 50 H eR = X aR 25 H R 1/2 = 0.6455 \hspace{1em} (A) \hspace{1em} (8)$$

In decibels, results in:

$$a F R 50 = 20 \log X aR 25 H R (db/m) \hspace{1em} (9)$$

NIST doesn't determine the receiving antenna input impedance but the receiving antenna capacity using the well known antenna capacity by the equation published by Schelkunoff and Friis [3,], or:

$$C aR = 2 ? 0 H ln(H/a) \hspace{1em} ? 1 \hspace{1em} (F) \hspace{1em} (10)$$

From this equation the capacitive reactance $X aR$ is obtained:

$$X aR = 12 f C aR \hspace{1em} (?) \hspace{1em} (11)$$

Using this procedure, where $R aR$ is negligible, the receiving antenna factor $a F R 50$ is reactive and practically imaginary. Here, the simulation is performed as an example at the frequency $f = 3$ (MHz) by means for a radio link between two monopole antennas with the same physical geometry like NIST. The input impedance of both monopoles is obtained by a WIPL-D software [6], or:

$$Z aT = (R aT + j X aT ) = (0.24 ? j2217) \hspace{1em} (?) \hspace{1em} (12)$$

$$Z aR = (R aR + j X aR ) = (0.24 ? j2637) \hspace{1em} (?) \hspace{1em} (13)$$

Transmitted power $W T$ depends from the radiation resistance $R aT$ and the squared current $I 2 T$ of the transmitting antenna and for a transmitted power $W T = 0.1$ (W), results in:

$$T = W T R aT 1/2 = 0.1 0.24 1/2 = 0.6455 \hspace{1em} (A) \hspace{1em} (14)$$

The voltage $V T$ on the radiation resistance $R aT$, results in:

$$V T = (I T R aT ) = 0.6455 ? 0.24 = 0.155 \hspace{1em} (V) \hspace{1em} (15)$$

The voltage $V Z aT$ on the transmitting antenna impedance $Z aT$, results in:

$$V Z aT = (I T Z aT ) = (V) \hspace{1em} (16)$$

$$Z aT = 0.6455 ? (0.24 ? j2217) = (0.155 ? j1431) \hspace{1em} (V) \hspace{1em} (17)$$

The voltage is complex with the real part very small compared to the imaginary part. Its module is obtained as:

$$| V Z aT | = 1431 \hspace{1em} (V) \hspace{1em} (18)$$

The voltage $V R g$ on the generator or amplifier impedance, in order to feed the transmitting antenna, results in:

$$V R g = (I T g R ) = 0.6455 ? 50 = 32.3 \hspace{1em} (V) \hspace{1em} (19)$$

This way, the voltage $V g$ from the generator or amplifier must be:

$$V g = (V R g + V Z aT ) = 1431 + 32.3 = 1463.3 \hspace{1em} (V) \hspace{1em} (20)$$

The necessary power $W g$ to produce the transmitting power $W T = 0.1$ (W), result in:

$$W g = (V g I T ) = 1463.3 ? 0.6455 = 944.56$$ (W) \hspace{1em} (21)

It is very important to see the low efficiency of the power supply when a transmitting antenna is very reactive and with no impedance matching. Almost 1 KW to radiate 100 mW. For this reason NIST uses a power amplifier to feed the transmitting short monopole. But it is the only way to feed a wide band short antenna at frequencies lower than 10 MHz. In simulation the voltage using WIPL-D to feed the transmitting antenna is $| V Z aT | = 1431$ (V) and transmitting gain, field strength and power density obtained at the distance $r = 30$ (m), are:

$$G_T = 4.$$ \hspace{1em} (22)

Current module $I R$ in the receiving antenna equivalent Thevenin circuit for $R L = 50$ (?), results in:

$$I R = V i L + X aR (A) \hspace{1em} R = 0.1117 + 50 + 2637 = 4.16 E ? 5 \hspace{1em} (A) \hspace{1em} (24)$$

The receiving voltage $V R 50$ , is obtained as:

$$V R 50 = 50 I R = 50 ? 4.16 E ? 5 = 208 E ? 3 \hspace{1em} (V) \hspace{1em} (25)$$

Receiving antenna factor $a F R 50$, results in:

$$a F R 50 = E i V R 50 = 8.936 ? 2.08 E ? 3 = 42.96 \hspace{1em} (1/m) \hspace{1em} (26)$$

The antenna factor $A F R 50$ in decibels is:

$$A F R 50 = (20 log a F R 50 ) = 32.66$$ (db/m) \hspace{1em} (27)

This is a pure imaginary antenna factor. If an antenna factor could be real, complex or imaginary, the area of
the receiving antenna could get the same characteristics because the power on the load impedance R L50 could be complex. Using the classical equation:

\[ A \text{eR} = W \text{R P} \cdot i(1/m) \]  

The power at the calibrated receiver input, results in:  

\[ W \text{R}50 = (R \text{L} \cdot i(1/m) \cdot 50 = (4.16 \text{E} \cdot 5) \cdot 2 = 8.65 \text{E} \cdot 8 \]  

And the effective area, results in:  

\[ A \text{eR} = W \text{R P} \cdot i(2/m) \]  

Numerical receiving antenna gain, according to Schelkunoff and Friis, results in:

\[ g \text{R} = 4 \cdot 2 \cdot A \text{eR} = 4 \cdot 10^2 \]  

The receiving antenna gain G R in decibels, results in:

\[ G \text{R} = 10\log 4 \cdot 2 \cdot A \text{eR} = 75.93 \text{dBi} \]  

The transmission loss a w in the radio link is obtained, as: The power transmission loss or site attenuation A w in decibels, results in:

\[ a \text{w} = W \text{R R T} \cdot A \text{w} = 10 \log a \text{w} = 760.63 \text{dBi} \]  

Free space A F S in decibels, results in:

\[ A \text{F S} = 10 \log 4 \cdot r = 2 = 715.13 \text{dBi} \]  

Gain and losses relationship, according to Schelkunoff and Friis, results in:

\[ g \text{T} + G \text{R} = 4.77 + (?753.93) \]  

Friis radio link power budget is fulfilled. Scattering gain in dB is calculated by software WIPL-D, as:

\[ G \text{S} = ?18.33 \text{dBi} \]  

Numerical scattered gain g s , results in:

\[ g \text{s} = 1.47 \text{E} \cdot 2 \]  

Scattering area is obtained by the isotropic radiator area A eo and the numerical scattering gain g s , as:

\[ A \text{eo} = 11.70 \text{m} \]  

Transmitting antenna effective area A eT , is obtained this way, knowing its numerical gain g T , or:

\[ A \text{eT} = ?24 \cdot ?g \text{T} = 2379.37 \text{m} \]  

Relation between areas and gain, according to Schelkunoff and Friis, are:

\[ A \text{eT} g \text{T} = A \text{eR} g \text{R} \]  

All cases are giving practically the same results. At this example of f = 3 (M Hz) in the radio link with a transmitted power W T = 100 (mW) the received voltage is V R50 = 2.08 E ? 3 (V) or V R50 = ?726.82 (dBV) in power W R50 = 8.65 E ? 3 (W) or W R50 = 770.63 (dBW) and the antenna factor AF R50 = 32.66 (dB/m). According to the reciprocity principle (Schelkunoff and Friis) is possible to calculate the transmitting antenna factor AF T 50, to be:

\[ AF \text{T} = 2 \cdot 4 \cdot Z \text{w} \cdot L \cdot g \text{T} = 4.99 \cdot 10^2 \cdot (1/m) \]  

in decibels:

\[ AF \text{T} = 20 \log 2 \cdot 4 \cdot Z \text{w} \cdot R \cdot L \cdot g \text{T} = 13.02 \text{dBi} \]  

For this example the relationship between factors, areas and gain for the monopole antennas for H T and H R = 2.5 (m), results in:

\[ AF \text{T} R = 24 \text{E} \cdot 3 \]  

thing to know is, in the case of the short antennas, the difference between identical antennas characteristics over ground are extremely different and not only 6 dB like in the case of resonant and perfectly matched identical antennas.  

Here is shown that the equation 7 in the Standard IEEE-ANSI C63.5-2004 cannot be used because the factors, area and gain are not the same for identical antennas when they are operating over perfect ground. Different procedures must be used. NIST (Technical Note 1347) ??122) have not calculated all the parameters obtained here in order to know the behavior of both antennas and their characteristics. Doing the same simulation for other frequencies the results are presented in Table ?? in this table it can be shown that the results obtained are practically identical to that obtained by NIST.

Transmitting antenna factor AF T was not defined as the receiving antenna factor AF R, or:

\[ AF \text{T} = E \cdot i \cdot V \text{R} \]  

However, is possible to determine the transmitting antenna factor by means of the Power Reciprocity Principle according to Schelkunoff and Friis:

\[ AF \text{T} = 2 \cdot 4 \cdot Z \text{w} \cdot L \cdot g \text{T} \]  

The effective area, results in:

\[ A \text{eT} = W \text{R} P \cdot i(1/m) \]  

This way, is possible to determine the relation between the receiving numerical antenna factor AF R and the receiving antenna numerical gain g R in the far field, or:

\[ AF \text{R} = 1 \cdot 4 \cdot Z \text{oo} \cdot g \text{R} \cdot L \cdot 1/2 (1/m) \]  

Power reciprocity principle presented by Schelkunoff and Friis, is expressed as:

\[ A \text{eT} g \text{T} = A \text{eR} g \text{R} \]  

According to the Receiving antenna factor definition:

\[ AF \text{R} = E \cdot i \cdot V \text{R} \]  

It is possible to determine the relation between the receiving numerical antenna factor AF R to the receiving antenna effective area A eR, in the far field when the impedance Z w = Z oo = 120 ? 377 (?), or:

\[ AF \text{R} = Z \text{oo} \cdot A \text{eR} \cdot L \cdot 1/2 (1/m) \]  

5 VIII. Transmitting Antenna Factor Definition

Receiving antenna effective area, in the far field, results in:

\[ A \text{eR} = ?24 \cdot R \cdot 4 \cdot (m) \]  

This equation is exactly the same as for the receiving antenna factor but instead of the numerical gain g R for the transmitting antenna the numerical gain g T must be used. At the same time, it is seen that these equations are that indicated by the Federal Communication Commission (F.C.C.) to calculate the antenna factors if the space intrinsic impedance Z oo = 120 ? 377 (?), wavelength in (m) and a load resistance R L = 50 (?).
For a transmitting antenna.

These equation are valid for a radio link in free space or over a perfect ground using the corresponding gain obtained in the indicated environment. Over perfect ground the maximum gain obtained for a theoretical half wave dipole antenna is \( G_T = 8.15 \text{ (dBi)} \) or very close to this value in an actual environment and \( G_R = 2.15 \text{ (dBi)} \) for a receiving half wave antenna at practically any height over perfect ground \(^{10}\). Around \( R aT = R aR = 73 \text{ (?)} \) is obtained for the radiation resistance of a resonant dipole. \((R aT = R aR = 70 \text{ to 73 (?)}) in practical thin dipoles. In the case of a theoretical quarter wave monopoles over perfect ground maximum gain for a transmitting antenna is \( G_T = 5.15 \text{ (dBi)} \) at zero elevation angle and \( G_R = 70.85 \text{ (dBi)} \) for the receiving antenna \(^{10}\). Around \( R aT = R aR = 34 \text{ to 36 (?)} \) of a radiation resistance is obtained in resonance for thin monopoles.

In conclusion is demonstrated that the antenna parameters in a radio link over perfect ground have a difference of 6 dB in favor of the transmitting antenna for perfect resonant and matched antennas, in the maximum radiation \(^{10}\). This is valid for any identical antenna used in the radio link. For not perfectly matched antennas this difference is even larger, as demonstrated previously, in this paper.

The comments that have been presented here show that a radio link, in free space or over perfect ground, using any kind of antennas, can be verified using the Friis equation and achieve the power budget and the power reciprocity principle in order to be sure that the radio link is working properly. No artificial factors are needed to obtain this result if the proper antenna gain is used \(^{7}, \text{[8]}\). In the case of a quarter wave monopole antenna its gain over a perfect absorbing surface has a theoretical gain of \( G_T = 70.85 \text{ (dBi)} \) (theoretically a real monopole). Over a perfect reflective surface its image increases its length to a half-wave (a real dipole), that in free space has a gain of \( G_T = 2.15 \text{ (dBi)} \). For this reason, a called monopole over perfect ground needs to only cover the half spherical space over ground and this increases its gain additionally by 3 (dB) achieving the well known gain of \( G_T = 5.15 \text{ (dBi)} \) and maintaining its radiation resistance in resonance \( R aT 36(?) \), because mutual effects are in free space and its logical gain \( G_T = 5.15 \text{ ??dbi} \). However, he said nothing about the characteristics of Rx quarter wave monopole antenna whose effective area is half the area of a half-wave dipole in free space and its logical receiving gain \( G_R = 70.85 \text{ (dBi)} \). This means 3 (dB) larger gain of a half-wave dipole antenna in free space who needs to cover all the spherical area with its radiated energy. This problem was solved in the thirthie’s in the golden AM BC era. In the receiving case its effective area is half that of the half-wave dipole in free space and from it, according to Schelkunoff and Friis, its receiving gain is \( G_R = 70.85 \text{ (dBi)} \), a true monopole without image. At the same time, any receiving antennas in the receiving role work like in free space, because no transmitting energy is arriving at its image if the surface is not transparent. Thus, it works practically independent of its height over ground and of its distance from the transmitting one. Of course, in scattering the Rx antenna works practically like a Tx antenna and its reradiation or scattering depends on its height over ground and with its image assistance. This also, is verified in the case of the monopole-dipole radio link where the gain of the monopole is \( G_T = 5.15 \text{ (dBi)} \) and the dipole over ground has a receiving gain, as was determined previously, of \( G_R = 2.15 \text{ (dbi)} \), practically constant like in free space. In all case analyzed, the power budget and the power reciprocity principle are fulfilled perfectly well without changing the natural antenna gains and showing the perfect radio link work. The Tx antenna gain, well known since the thirties, add 6 db at its gain compared to the gain of the same antenna in free space. This depends of the image effect like in the monopole antenna case. These results have been corroborated experimentally in the RF spectrum in MF, HF, VHF and UHF confirming that the Rx antenna in the receiving role works without the image effect or like in free space. It was determined that in the short monopole antenna case the difference between identical antennas in transmission and reception is extremely greater than in the case of resonant and well matched antennas and not only 6 dB. Here it is shown that over perfect or natural ground identical antennas have always different characteristics as factor, area and gain. It is also important to know that: the antenna area \( A eT A eR \) and gain \( g T g R \) are parameters valid accurately in far field \( r \) when the wave impedance \( Z \) is really \( Z = 120? \) and the effective length \( L eR \) or height \( H eR \) and the antenna factor \( aF T aF R \) is a parameter inherent of the antenna, for this reason they are practically constant from the distance or height over ground. However, these parameters can be related between them in the far field.

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6 Aknowledgement

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\(^{1}\) ( ) H © 2022 Global Journals
Figure 1: Figure 1.
Figure 2: Figure 2.

Figure 3: Figure 3.
Figure 4:
[Kraus et al. (1950)] J D Kraus, Antennas Mc, N Y Hill. 1950.


