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LWE Encryption using LZW Compression

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LWE Encryption using LZW Compression

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I. INTRODUCTION

Secure transmission of data has become the key for successful completion of all transactions. NTRU Labs have created a bench-mark in secure transmission of data using a ring of truncated polynomials [1, 2, 3, 4]. Many attempts have been made to break the crypto-systems based in NTRU technique; but no successful attempt has ever been reported. However polynomial inversions are difficult to perform in modulo-arithmetic. Moreover, polynomials are to be repeatedly chosen until they could be properly inverted.

In the last three to four years, Learning With Errors (LWE) has emerged as a versatile alternative to the NTRU cryptosystems. All cryptographic constructions based on LWE [5, 6, 7] are as secure as the assumption that SVP (Smallest Vector Problem)[8,9] is hard on integer lattices.

The LWE problem can be stated as follows:

Recover s, given $A \cdot s \cong b$ where $s \in Z_q^n$, $b \in Z_q^n$ and A is $m \times n$ matrix with m > n and Z_q^n is set of integer vectors of size n and modulo q. In other words, we are given a set of m equations in n unknowns and the right hand side slightly perturbed with the error vector chosen from normal distribution χ with low standard deviation. More precisely we say that an solves LWE[10] if we can recover s, given that the errors

are distributed according to the error distribution χ and the elements of A are chosen uniformly at random from Z_a^n [10].

The number of equations or the number of rows in the matrix is irrelevant since additional equations can be formed that are as good as new, by adding the given equations.

One way to obtain a solution to the LWE problem is to repeatedly form new equations until we get the first row of the matrix A as $(1, 0, 0, 0, \ldots, 0)$ which gives a solution to the first component of s. We can repetitively apply the same procedure for the other components of s. However the probability of obtaining such a solution is almost nil, of the order of q^{-n} , and the set of equations needed are $2^{O(n \log n)}$ and with a similar running time.

The algorithm can be stated as follows:

Private Key: s, chosen uniformly at random from Z_q^n .

Public Key: m samples of (A_i, b_i).

Encryption: for each bit of the message, we chose at random a set T from the 2^m subsets of the m equations. The encryption is $(\sum_{i \in T} A_i, \sum_{i \in T} b_i)$, if the bit is zero and the encryption is $(\sum_{i \in T} A_i, \left|\frac{q}{2}\right| + \sum_{i \in T} b_i)$ if the bit is 1. *Decryption:* The decryption of the pair (a, b) is 0 if $b - \langle a, s \rangle$ is closer to 0 than to $\left|\frac{q}{2}\right|$, 1 otherwise.

However, transmitting a text with bitwise encryption will be cumber-some and time-taking. We use a slightly modified version of the algorithm to encrypt '*l*' bits simultaneously. We choose A, S uniformly at random from $Z_q^{m \times n}$ and $Z_q^{n \times l}$ respectively and S is the private key. We generate the error matrix $E \in Z_q^{m \times l}$ by choosing each entry according to normal distribution $\chi \alpha$, where α is a measure of standard deviation which is usually chosen as $\sqrt{\alpha q}$ and α is small. The public key is (A, B) where B = A.S + E.

Farther simplification is made by choosing the elements of A in the form of a circulant matrix. In other words we have chosen A as [11]

<i>a</i> ₁	a2	a_3	a_4					a_n
a_2	a_3	a_4	a_5					$-a_1$
a 3	1 4	a_5	2 ₆		•	•	$-a_1$	$-a_2$
•				•	•	•	•	(k_{1},\ldots,k_{n})
•					•		•	(k_{1},\ldots,k_{n})

Let v be a vector belonging to message space Z_t^l . Choose a vector $a \in \{-1, 0, 1\}^m$ uniformly at random. The cipher text u corresponding to the

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message v is $(u = A^T a, C = B^T a + f(v))$ where f is an invertible mapping from the message space Z_t^l to Z_q^l and in this paper we have chosen the mapping as a multiplication of each co-ordinate by q/t and rounding to the nearest integer.

The original message can be recovered from the cipher text (u, C) using the private key S as $f^{-1}(C - S^T u)$ which can be seen as follows:

$$f^{-1}(C - S^{T} u) = f^{-1}(B^{T}a + f(v) - S^{T} A^{T}a)$$

= $f^{-1}((AS + E)^{T}r + f(v) - S^{T} A^{T}a)$
= $f^{-1}(E^{T}a + f(v))$
= $f^{-1}(E^{T}a) + v$

If a decryption error is to occur, say in the first letter, the first co-ordinate of $E^T a$ must be greater than q/(2t) in absolute value the probability of which is shown to be negligible [11].

However, some pre-processing of data greatly helps to reduce the time for encryption and decryption as well as time for transmission. We choose to compress the data before encryption using LZW (Lemple-Ziv-Welch)[12,13,14] technique and encrypt the reduced text. The LZW method of compression is based on dictionary structure. It creates a dictionary of its own for each character or a string of the input text. It is known to be a lossless compression and the percentage of reduction in the text is approximately 40% [15].

Another frequently used compression algorithm is the well known Huffman Technique [16,17,18] which constructs a binary tree based on the frequency of the occurrence of the letters and the corresponding code is generated. We have also used Huffman algorithm on the same text and compared the two compression technique used with LWE.

II. Illustration of the Proposed Algorithm

The parameters of the proposed algorithm are chosen as q = 2003, t = 2, n = 136, l = 136, alpha = 0.0065 and m = 2008 [11]

Original text message

str: wild animals, rocks, forest, beaches, and in general those things that have not been substantially altered by human intervention, or which persist despite human intervention.

The Compressed message using LZW is cmes=



Where the integers indicate the indices to the patterns generated by the compression algorithm.

Then we convert the message vector as obtained above into a binary

 $A \in \mathbb{Z}_{a}^{m \times n}$ is chosen as

1591	757	1974		1216	1991
757	1974	892		1991	-1591
1974	892	1760		-1591	-757
1137	1368	375		-887	-1301
1368	375	449		-1301	-1137
375	449	154		-1137	-1368

 $S \in \mathbb{Z}_q^{n \times l}$ is as follows

1759	2	154		1044	1218
764	1434	996		1703	945
475	1846	462		956	1644
136	591	1728		1489	708
782	945	84		121	1215
1271	916	1500		1439	76

 $E \in \mathbb{Z}_q^{n \times l}$ is as follows

<u> </u>						-		
-3	0	-1				2	3	
-2	0	0				0	0	
-3	-1	-2				-3	0	
•							•	
							-	
-7	4	-1				8	1	
-2	-2	0				2	-6	
-4	1	4				-1	2	
$B = A \times S + E(mod q) =$								

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1637	130	771		671	453
908	123	438		1399	264
527	963	184		1573	61
•					
720	312	299		1955	130
403	389	357		1428	1659
277	1467	1094		1056	39

Let $a = \{-1, 0, 1\}^m$ where the elements are chosen randomly.

-1	0	-1	-1	ć	í.		0	1	1 1	,
	0	C = E	$\mathbf{B}^T \times$	a +	f(ı	v)(r	nod q) =		
98	1396	40	81	049			291	1356	193	٦

 $u = A^T \times a \ (mod \ q) =$

314 1840 1588 148 . . . 988 1447 1125 $D = C - S^T \times u \pmod{q} =$ 1952 1992 . 15 1998 143 13 58 D/(q/t) =0 1 0 1 1 1 1 0 1 0 0 0 0 1 . 0 0 1 0 1 0

Convert binary to decimal

87 105 108 100 . . . 87 105 108 100

When the compression process is reversed we get the original message:

III. EXPERIMENTAL RESULTS

The following table gives the total execution time taken for a direct encryption and decryption, encryption and decryption after a LZW compression and encryption and decryption after a Huffman compression:

File Size in KB	Total Execution time without Compression	Total Execution time with LZW	Total Execution time with Huffman
1	3.13	2.4289	2.10777
2	10.84	5.3588	4.28654
3	16.26	8.1736	6.56431
4	21.63	10.9583	8.90506
5	27.00	14.7273	11.39183
6	32.43	18.2190	13.98658



IV. Conclusions

In this paper we have used ring-LWE to encrypt an input text. The text to be transmitted has been initially compressed using LZW Technique and the compressed text is encrypted using LWE. We have also used Huffman coding algorithm for compression for comparison purpose. It has been observed that compressing the input text greatly reduces the total time of transmission and Huffman coding works out to be better.

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