



Two-Party Threshold Key Agreement Protocol for Manets using Pairings

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Two-Party Threshold Key Agreement Protocol for Manets using Pairings

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Abstract In MANET environment, the nodes are mobile i.e., nodes move in and out dynamically. This causes difficulty in maintaining a central trusted authority say Certification Authority CA or Key Generation Centre KCG. In addition most of cryptographic techniques need a key to be shared between the two communicating entities. So to introduce security in MANET environment, there is a basic need of sharing a key between the two communicating entities without the use of central trusted authority. So we present a decentralized two-party key agreement protocol using pairings and threshold cryptography ideas. Our model is based on Joux's three-party key agreement protocol which does not authenticate the users and hence is vulnerable to man-in-the-middle attack. This model protects from man-in-the-middle attack using threshold cryptography.

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1. INTRODUCTION

Wireless technology [22] is suitable of communicating virtually every location on the plane of the earth. Most of the people exchange information every day using pagers, cellular telephones, laptops, several types of personal digital assistants (PDAs) and other wireless communication products. A Mobile Ad hoc NETWORK (MANET) is one that comes into practice as needed, without the support of existing infrastructure or any other kind of fixed stations. MANET is an independent system of mobile hosts (also serving as routers), connected by wireless links. In a MANET, no infrastructure exists and the network topology may dynamically change in an unpredictable manner since nodes are free to move. The important natural characteristics of MANETs [22] include frequently changing Topology, Lack of Central Administration, Battery Power supply or Restricted Energy, Restricted bandwidth, Physical Security fear.

Ad hoc networks are particularly prone to malicious behavior. Lack of any centralized network management or certification authority makes these dynamically changing wireless structures extremely vulnerable to penetration, eavesdropping, interference,

and so on. Security [22] is considered to be the major "barrier" in the commercial use of this technology. Security is indeed one of the most difficult problems to be solved in these networks due to lack of centralized network management. Most of the security mechanisms essentially require a secret key or session key or master key to be shared between the two communicating entities. So there is a need to share a key between the sender and receiver without the use of centralized network management or certification authority.

Key agreement is one of the basic cryptographic essentials. This is needed in cases where two or more users want to communicate securely among themselves. The first two-party key sharing protocol was introduced by Diffie-Hellman. Since its detection in 1976, the Diffie-Hellman protocol [1] has become one of the most well-known and mostly used cryptographic primitive. In its basic version, it is an efficient solution to the problem of creating a common secret between two participants. Since this protocol is also used as a building block in many complex cryptographic protocols, finding a generalization of Diffie-Hellman would give a new tool and might lead to new and more efficient protocols. But this is an unauthenticated protocol in the sense that an adversary who has control over the communication channel can use the man-in-the-middle attack to share two separate keys with the two users, without the users being aware of this. In this paper, we present a secure two-party key agreement protocol that protects from man-in-the-middle attack. Our protocol is based on Joux's protocol [1] which in turn is the generalization of Diffie-Hellman protocol.

One round tripartite key agreement Joux's protocol [1] uses Weil and Tate Pairings and the idea of Diffie-Hellman. These pairings were first used in cryptology as cryptanalysis tools to decrease the complexity of the discrete logarithm problem on some "weak" elliptic curves, but they are also used today to build cryptographic systems.

In this paper, we present a secure two-party key agreement protocol for MANET environment. This model extends the popular known Joux's tripartite key agreement protocol [1] to two-partite with minor modifications. Similar to Joux model [1], this model uses pairings or bilinear maps, unlike Joux this model uses threshold cryptography. Recently Pairing-based

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cryptography in the form of Identity-based cryptography has become a highly working research issue.

The paper is organized as: Section II discusses on the background fundamentals needed to understand the proposed model. Section III discusses on the previous work done to share a key between two entities using pairings. Section IV talk about the detailed description of the proposed model. Section V gives the software implementation of the proposed model and Section VI confers the conclusion and future enhancements that can be done to improve the model.

II. PRELIMINARIES

a) Bilinear Maps

The bilinear map was proposed originally as a tool for attacking elliptical curve encryption by reducing the problem of discrete algebra on an elliptical curve to the problem of discrete algebra in a finite field, thereby reducing its complexity. However, this method has been used recently as an encryption tool for information protection, instead of an attacking tool. Bilinear pairing is equivalent to a bilinear map.

Consider two additively written abelian groups A_1 and A_2 ; the identity element being 0. Also consider a multiplicatively written cyclic group C ; the identity element being 1. A pairing [2][17] on A_1 , A_2 and C is a non-degenerate, bilinear map

$$e : A_1 \times A_2 \rightarrow C.$$

A bilinear pairing e is a function which maps a pair of points on an elliptic curve E , defined over fields A_1 and A_2 , to an element of the multiplicative group of a finite extension field C . This mapping is said to be pairing as it maps a pair of elliptic curve points. The pairing e has the following characteristics:

Non-degenerate: Given a point $\mathcal{O} \neq X \in A_1$ there exists a point $Y \in A_2$ such that $e(X, Y) \neq 1$; Where \mathcal{O} is the point at infinity on the elliptic curve over the finite field A_1 .

Bilinear: for all points $X, X_1, X_2 \in A_1$, and $Y, Y_1, Y_2 \in A_2$ and $u, v \in \mathbb{Z}$ we have

$$\begin{aligned} e(X_1 + X_2, Y_1) &= e(X_1, Y_1) e(X_2, Y_1), \\ e(X_1, Y_1 + Y_2) &= e(X_1, Y_1) e(X_1, Y_2). \end{aligned}$$

This can be redefined in the following way:

$$e([u]X, [v]Y) = e(X, Y)^{uv} = e([v]X, [u]Y);$$

where $[u]X = X + X + \dots + X$ (u times)

Computable: There exists a computationally efficient algorithm to find $e(X, Y)$ for all $X \in A_1$ and $Y \in A_2$.

Laws of Bilinear Pairings: The following equations holds good for the bilinear pairing e . Consider $X \in A_1$, and $Y \in A_2$ and $u, v \in \mathbb{Z}$ and \mathcal{O} is the point at Infinity.

$$\begin{aligned} e(X, \mathcal{O}) &= e(\mathcal{O}, Y) = 1 \\ e(-X, Y) &= e(X, Y)^{-1} = e(X, -Y) \\ e([u]X, Y) &= e(X, Y)^u = e(X, [u]Y) \\ e([u]X, [v]Y) &= e(X, Y)^{uv} \end{aligned}$$

Some of the examples of cryptographic bilinear maps are Weil Pairing [11] and Tate Pairing [5]. Pairings in elliptic curve cryptography are functions which map a pair of elliptic curve points to an element of the multiplicative group of a finite field.

There are two types of pairings commonly used in the cryptography literature. The first type of pairing called Symmetric Pairings are of the form

$e : A_1 \times A_1 \rightarrow C$, where A_1 and C are cyclic groups of prime order p written additively and multiplicatively respectively.

The second type of pairing called Asymmetric Pairings are of the form

$e : A_1 \times A_2 \rightarrow C$, where A_1, A_2 are additively written cyclic groups of prime order p and C is a multiplicatively written cyclic group of prime order p .

The first form is just the special case with $A_2 = A_1$. Asymmetric Pairings are further divided into two types and hence leading to totally three types of Pairings [19]

Type 1: $A_1 = A_2$ Symmetric Pairing;

Type 2 : $A_1 \neq A_2$ Asymmetric Pairing but there is an efficiently computable homomorphism function $\psi : A_2 \rightarrow A_1$;

Type 3 : $A_1 \neq A_2$ Asymmetric Pairing and there are no efficiently computable homomorphism functions between A_1 and A_2 .

b) Threshold Cryptography

Let t and n be positive integers, $t \leq n$. A (t, n) -threshold scheme [25] is a method of sharing a secret K among a set of n participants in such a way that any t participants can compute the value of the secret, but no group of $t-1$ or fewer can do so.

Let the set of participants be denoted by E . The value of the secret K is chosen by the dealer, denoted D , who is a special participant not in E . When D wants to share the secret K among the participants in E , D gives each participant some partial information, called a share. The shares are distributed secretly, so no participant knows any other participant's share.

At a later time, when some qualified subset of participants $F \subseteq E$ want to compute the secret K , they will then pool their shares together. The most famous construction of a (t, n) -threshold scheme, called the Shamir Threshold Scheme [18][21], is invented in 1979. Therefore, a (t, n) threshold secret sharing scheme can protect the secret against an adversary who can intercept at most $t-1$ paths. In the proposed model D don't want to share the secret K among several participants in E , but D wants to share the key with the other end of communication say G , with whom he wants a secure communication. So D sends the shares of the secret key K through n independent paths [24] to G . When G receives at least t shares, he can recover the secret and there by a key is shared between D and E .

The opponent is facing the challenge of getting at least t shares by intercepting t paths at the same time, unless until he cannot recover the secret key.

III. RELATED WORK

There are many key agreement protocols based on bilinear maps, and later most of them have been broken. One of the first applications of pairing based cryptography was a tripartite key agreement protocol given by Joux [1]. This key agreement protocol does not authenticate the users, and thus is subject to the attack namely man-in-the-middle. Of course, it was an important step in the advancement of pairing based cryptography. This protocol only uses pairings especially Tate pairing but does not use identity-based cryptography.

Many key agreements from bilinear maps and identity based cryptography have been since proposed. Scott [7], Smart [8], and Chen and Kudla [6] have proposed two-party key agreement protocols, none of which have been broken. All of these schemes require that all parties involved in the key agreement are clients of the same Key Generation Centre (KGC). Nalla recommends a tripartite identity-based key agreement in [9], and Nalla and Reddy recommends a authenticated tripartite identity-based key agreement scheme in [10], but both have been broken down [12, 13]. Shim presents two key agreement protocols [14, 15], but both of these schemes have been broken by Sun and Hsieh [16]. Another authenticated tripartite key agreement protocol recommended by Al-Riyami and Patterson [3] was broken by Shim [4]. Cullagh and Barreto recommend a two-party identity based authenticated key agreement. Most of the above protocols are based on identity-based cryptography.

Our proposed model is based on Joux's Protocol [1]. It uses bilinear maps (Pairings) and Threshold cryptography concepts. It does not uses Identity based cryptography(IDC) because IDC needs the use of Key Generation Centre (KCG), a centralized controller and which is infeasible in MANETS environment .

a) Joux's Protocol

Joux Protocol [1] considers the three communicating parties A, B and C want to share a secret key K_{ABC} among them. Let A, B and C chooses random integers $u, v, \text{ and } w \in \mathbb{Z}_q^*$ respectively. Consider the Symmetric Pairing $e: A_1 \times A_1 \rightarrow C$ and P is the generator of the cyclic group A_1 publicly known. The Protocol continues as follows and shown in Fig. 1:

1. $A \rightarrow B, C$: $[u]P$
2. $B \rightarrow A, C$: $[v]P$
3. $C \rightarrow A, B$: $[w]P$
4. A computes $K_A = e([v]P, [w]P)^u$

5. B computes $K_B = e([u]P, [w]P)^v$
6. C computes $K_C = e([u]P, [v]P)^w$

From the laws of bilinear pairings, K_A, K_B, K_C result in the same value, say K_{ABC} . So common agreed key of A, B, C $K_{ABC} = K_A = K_B = K_C = e(P, P)^{uvw}$.

- *Assumption* : Bilinear Diffie-Hellman (BDH) [2] [Sec. 3.2.] problem is hard to compute.
- *Security* : Secure against passive opponent under the assumption that BDH problem is hard.
- *Efficiency* :
- *Communication* : Number of Rounds required is 1; number of group elements sent are 3.

Computation : 3 scalar multiplications; 3 pairing computations; 3 exponentiations.

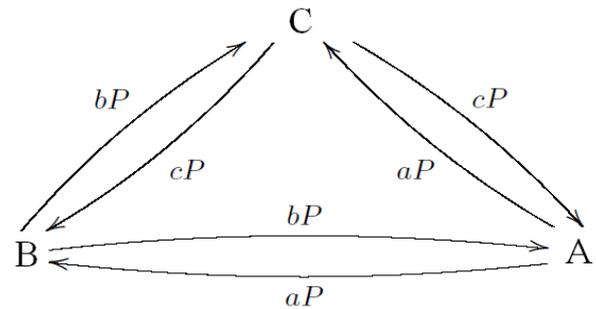


Figure 1: Joux's Tripartite Key Agreement

b) Diffie-Hellman Assumption

In this subsection we specify the version of the Diffie-Hellman problem which we will require. Consider the triple $\langle A_1, C, e \rangle$ where A_1, C are two cyclic subgroups of a large prime order q and $e: A_1 \times A_1 \rightarrow C$ is a cryptographic bilinear map. We take A_1 as an additive group and C as a multiplicative group.

Bilinear Diffie-Hellman BDH Problem

The strength of Joux's protocol is based on the Bilinear Diffie-Hellman (BDH) [2] assumption. Let P be the generator of A_1 and a, b, c are positive integers

. The BDH assumption considers the computation of $e(P, P)^{abc}$ given $\langle P, aP, bP, cP \rangle$ to be hard.

c) Man-in-the-middle Attack

Let three parties A, B, C respectively have chosen secrets at random $u, v, w \in \mathbb{Z}_q^*$ and let D be the attacker chooses three random secrets u', v', w' and let D be the Consider the Symmetric Pairing $e: A_1 \times A_1 \rightarrow C$ and P is the generator of the cyclic group A_1 publicly known. The attack functions as follows:

1. $A \rightarrow B, C$: $[u]P$.
D intercepts $[u]P$ and instead sends $[u']P$ to B, C.
2. $B \rightarrow A, C$: $[v]P$.
D intercepts $[v]P$ and instead sends $[v']P$ to A, C.

3. $C \rightarrow A, B: [w]P$.
 D intercepts $[w]P$ and instead sends $[w']P$ to A, B.
4. A computes $K_1 = e([w']P, [v']P)^u = e(P, P)^{u'v'w'}$.
 D computes $K_1 = e([u]P, [v']P)^{w'} = e(P, P)^{u'v'w'}$.
5. B computes $K_2 = e([u']P, [w']P)^v = e(P, P)^{u'vw'}$.
 D computes $K_2 = e([v]P, [w']P)^u = e(P, P)^{u'vw'}$.
6. C computes $K_3 = e([u']P, [v']P)^w = e(P, P)^{u'v'w}$.
 D computes $K_3 = e([u']P, [w]P)^v = e(P, P)^{u'v'w}$.

Finally instead of a key shared between three users A, B and C, three keys are shared among four users A, B, C and D where one key K1 between A and D, another K2 between B and D and another K3 between C and D.

IV. PROPOSED MODEL

One of the applications of Joux's protocol is to share a master key between two communicating parties and one central authority say certification Authority CA or Public Key Generator PKG. MANET environment lacks central management and hence there is need for two-party key agreement protocol. Our proposed two party key agreement algorithm is based on Joux's Protocol. It makes use of Pairings (or Bilinear Maps) and Threshold cryptography concepts. Let A and B be the two communicating parties want to share a secret or session key. Let A, B respectively select integers at random $u \in \mathbb{Z}_q^*$.

1. $A \rightarrow B: [u]P$
2. $B \rightarrow A: [v]P$
3. A computes $e(P, [v]P)^u = e(P, P)^{uv}$.
4. B computes $e([u]P, P)^v = e(P, P)^{uv}$.

If $R=[u]P$ and $S=[v]P$ are transmitted as is without applying threshold cryptography as shown in Fig 2., adversary can easily compute the key as $e([u]P, [v]P) = e(P, P)^{uv}$ by just intercepting $[u]P$ and $[v]P$ during steps 1 and 2.

To counter this we apply the concept of threshold cryptography for steps 1 and 2; steps 3 and 4 remain the same. The secrets 'u' and 'v' are split into n shares each using Shamir's secret sharing mechanism [21] to get u_i and $v_i \forall 1 \leq i \leq n$, where n is the number of multiple independent paths that exist between sender and receiver. The shares of the products $[u] P$ and $[v]P$ are then calculated as $R_i = [u_i]P$ and $S_i = [v_i]P$. These shares are then exchanged through n independent paths with the other party as shown in Fig 3. The n independent paths used to transmit $[u_i]P$ and $[v_i]P$ are

the same, but shown differently in Fig 3 for easy understanding.

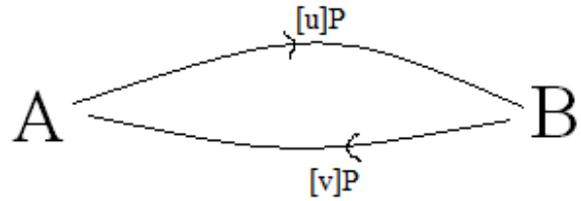


Figure 2 : $[u]P$ and $[v]P$ exchanged between A and B without Threshold Cryptography (i.e without dividing into n shares)

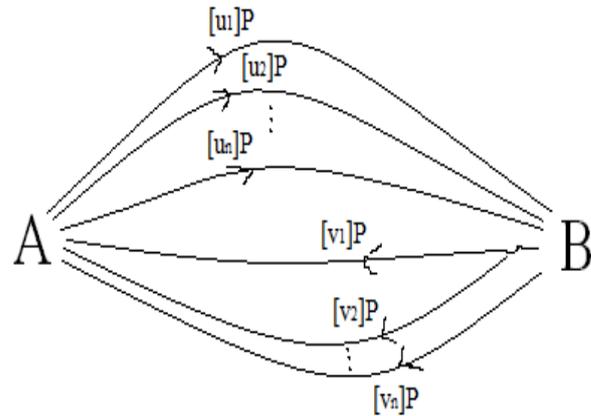


Figure 3 : The n shares of $[u]P$ and $[v]P$ exchanged between A and B over n independent paths

When A and B receives at least t shares of S_i and R_i respectively, they can reconstruct S and R as

$$R = \sum_{i=1}^t R_i \prod_{1 \leq m \leq t, m \neq i} \frac{m}{i-m}$$

$$S = \sum_{i=1}^t S_i \prod_{1 \leq m \leq t, m \neq i} \frac{m}{i-m}$$

Hence unless the adversary intercepts at least t shares of R_i and S_i , he cannot reconstruct R and S and therefore the key. Also the key is the session key that has small life time i.e., over a single session; hence the time scope for adversary to reconstruct the key is small, thereby protecting the protocol from man-in-the-middle attack.

V. IMPLEMENTATION

The proposed key agreement protocol is implemented in software using the Pairing-Based Cryptography Library (PBC) [20]. The results are as follows:

The Elliptic curve is chosen as: $y^2 = x^3 + x$, with x, y elements of a Field F_q ; q is a prime number. A1 is a subgroup of $E(F_q)$. C is a subgroup of F_q^2 . There are q+1 points on the ECC curve, i.e. $\#ECC(F_q) = q+1$. We consider symmetric bilinear map $A1 \times A1 \rightarrow C$.

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