

Fuzzy Conditional Inference and Application to Wireless Sensor Network

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Abstract

Zadeh, Mamdani, and TSK were proposed different fuzzy conditional inference for "if ? then ?" to approximate incomplete information. The Zadeh and Mamdani fuzzy conditional inferences require prior information for the consequent part. The TSK fuzzy conditional inference need not to know prior information for the consequent part, but it is difficult to compute. In this paper, new method is proposed for the position containing "if ? then ?" when prior information is not know the consequent part. Fuzzy Wireless Sensor Networks are discussed an application for proposed fuzzy conditional inference. Fuzzy inference system (FIS) is also discussed for WSN to detect Coastal erosion and Turbo Charger fuzzy controls System an examples.

Index terms— fuzzy logic; fuzzy conditional inference; fuzzy control systems; wireless sensorn networks; costal erosions.

1 Fuzzy Conditional Inference and Application to Wireless Sensor Network

Poli Venkata Subba Reddy Abstract-Zadeh, Mamdani, and TSK were proposed different fuzzy conditional inference for "if ? then ?" to approximate incomplete information. The Zadeh and Mamdani fuzzy conditional inferences require prior information for the consequent part. The TSK fuzzy conditional inference need not to know prior information for the consequent part, but it is difficult to compute. In this paper, new method is proposed for the position containing "if ? then ?" when prior information is not know the consequent part. Fuzzy Wireless Sensor Networks are discussed an application for proposed fuzzy conditional inference. Fuzzy inference system (FIS) is also discussed for WSN to detect Coastal erosion and Turbo Charger fuzzy controls System an examples.

2 II.

3 Fuzzy Logic

Zadeh [11] introduced the concept of a fuzzy set as a model of a vague fact. Fuzzy set theory for control systems is accepted because it is very convenient and believable. The fuzzy set may be defined with membership function or commonsense. Definition: Given some universe of discourse X, a fuzzy set A of X is defined by its membership function μ_A taking values on the unit interval [0,1] i.e $\mu_A : X \rightarrow [0,1]$ Suppose X is a finite set. The fuzzy set A of X may be represented as $A = \mu_A(x_1)/x_1 + \mu_A(x_2)/x_2 + \dots + \mu_A(x_n)/x_n$

Where "+" is union For instance, fuzzy set may be defined with commonsense TALL = 0.00/5'0" + 0.08/5'4" + 0.32/5'8" + 0.50/6'0" + 0.82/6'4"

There is an alternative way to defined fuzzy subset with function and is given by [7] For instance, fuzzy set may be defined with membership function YOUNG = { $\mu_{YOUNG}(x)/x=1$ if $x \in [0,25]$ = $[1 + ((x-25)^2)^{-1}]$ if $x \in [25,100]$ }

42 Let A and B be the fuzzy sets, and the operations on fuzzy sets are given below
 43 $AVB = \max(\mu A(x), \mu B(y))$
 44 Disjunction $A \cup B = \max(\mu A(x), \mu B(y))$ Conjunction $A \cap B = \min(\mu A(x), \mu B(y))$ Negation $\neg A = 1 - \mu A(x)$
 45 Implication $A \rightarrow B = \min\{1, (1 - \mu A(x) + \mu B(y))\}$ Relation $A \circ R = \min_x \{\mu A(x), \mu R(x,y)\}$

45 **4 y Composition**

46 **5 Implication**

47 The Zadeh fuzzy condition inference is given by if x_1 is A_1 and x_2 is A_2 and $?$ and x_n is A_n then y is $B =$
 48 $\min\{1, (1 - \min(\mu A_1(x_1), \mu A_2(x_2), \dots, \mu A_n(x_n)) + \mu B(y))\}$ For Example $A_1 = 0.2/x_1 + 0.6/x_2 + 0.9/x_3 +$
 49 $0.6/x_4 + 0.2/x_5$

50 **6 Introduction**

51 here are many theories to approximate incomplete information. Until recently, probability theory was the
 52 only existing theory to the approximate incomplete formation. Zadeh [11] proposed to deal with incomplete
 53 information. A Fuzzy set allows us to represent membership function as possibility distribution. Fuzzy theory is
 54 the most effective than the other theory because fuzzy theory depends on the degree of belief rather than likelihood
 55 (Probability). Fuzzy conditional propositions are of the type if (precedent part) then (consequent part). There
 56 are different methods of fuzzy conditional inference to approximate uncertain information [2,3,4,6,7]. The Zadeh
 57 and Mamdani inferences are needed prior information for both precedent and consequent part. There are some
 58 applications like fuzzy control systems that do not have prior information to the consequent part. The TSK fuzzy
 59 conditional inference need not know prior information to the consequent part, but it is difficult to compute.

60 The Sensors are able to sense and process the data. The Sensors are used to collect the data or information
 61 for many application like Wireless Sensor Networks and Control Systems. The Wireless Sensor Network (WSN)
 62 and fuzzy control systems are given as examples for proposed fuzzy conditional inference. It is necessary to
 63 give a brief description of fuzzy logic and WSN.

64 $T A_2 = 0.5/x_1 + 0.7/x_2 + 0.9/x_3 + 0.7/x_4 + 0. = 0.9/x_1 + 0.8/x_2 + 0.7/x_3 + 0.8/x_4 + 0.9/x_5$
 65 Mamdani fuzzy inference is given as $\min(A_1, A_2, \dots, A_n, B) = 0.1/x_1 + 0.4/x_2 + 0.6/x_3 + 0.4/x_4 + 0.1/x_5$
 66 5

67 Mamdani inference is given as if x_1 is A_1 and x_2 is A_2 and $?$ and x_n is A_n then y is $B = \min(A_1, A_2, \dots, A_n, B)$
 68 Reddy [7] fuzzy inference is given as if x_1 is A_1 and x_2 is A_2 and $?$ and x_n is A_n then y is $B =$
 69 $\min(A_1, A_2, \dots, A_n)$

70 The "consequent" part is derived from "precedent" part of fuzzy conditions. $\min(A_1, A_2, \dots, A_n) = 0.2/x_1$
 71 $+ 0.6/x_2 + 0.9/x_3 + 0.7/x_4 + 0.3/x_5$

72 The Graphical representation of fuzzy inference is shown in Fig. ??.

73 **7 Fig. 2: Composition**

74 **8 Composition**

75 If some relation R between A and B is known and some value A_1 then B_1 is to infer from $R B_1 = A_1 \circ R = \min_x$
 76 $\{\mu A_1(x), \mu R(x,y)\}/(x,y)$, where $R = A \rightarrow B$ if $x = y$ $B_1 = A \circ R = \min\{\mu A_1(x), \mu R(x)\}/x$ According to Zadeh
 77 fuzzy conditional inference $B_1 = A_1 \circ R = \min\{\mu A(x), \mu R(x)\} = \min\{\mu A(x), \min(1, 1 - \mu A_1(x) + \mu B(x))\}$
 78 According to Mamdani fuzzy inference $= \min\{\mu A_1(x), \mu A(x), \mu B(x)\}$

79 If some relation R between A and B is not known According to The proposed fuzzy inference $= \min\{\mu A_1(x),$
 80 $\mu R(x)\}$ III.

81 **9 Wireless Sensor Technology**

82 Natural calamities are unpredictable and happen within short periods. Therefore WSN technology [1] used to
 83 capture signals and transmitted by monitoring. Wireless sensor technology that can send the sensed data to a
 84 data analysis center.

85 Fuzzy Inference System may be used as an alternative procedure. The capture data may be analyzed using fuzzy
 86 parameters, and these parameters are used in fuzzy inference system. Fuzzy inference system is applied to WSN
 87 to detect Coastal erosion.

88 WSN technology has the capability of capturing and transmission of critical data in real-time. The most
 89 common forms are minimum spanning trees for wireless networking sensors. Shortest paths: Minimal spanning
 90 tree is the shortest path connecting all the nodes with minimum distance. The Prim's algorithm may be used to
 91 construct minimum spanning tree. The minimum spanning tree has the base node and destination node. The
 92 data is transmitted from destination node to the base server.

93 The Prim's algorithm is to find a minimum spanning tree with nodes and edges. The nodes (V) are Sensors,
 94 and edges (E) are distances in WSN. Algorithm Prim(G) $G(V,E)$ is a weighted connected Graph $E \subseteq T$ is a set of
 95 edges of a minimum spanning tree $V \subseteq T$ is the initial node with any vertex Mamdani [2], and TSK [3,4] proposed
 96 fuzzy conditional inference for incomplete information. Zadeh and Mamdani's inferences need prior information

97 for the consequent part in "if ? then ?" if x_1 is A_1 and x_2 is A_2 and ? and x_n is A_n then y is B Zadeh fuzzy
98 inference is given by $= \min(1, \min(A_1, A_2, \dots, A_n) + B)$

99 The proposed fuzzy conditional inference for Zadeh fuzzy inference as when consequent part is not known =
100 $\min(1, 1 - \min(A_1, A_2, \dots, A_n + 1))$, where $B=1$ because B is not known.

101 For instance $A_1 = 0.2/x_1 + 0.6/x_2 + 0.9/x_3 + 0.6/x_4 + 0.2/x_5$ $A_2 = 0.5/x_1 + 0.7/x_2 + 0.9/x_3 +$
102 $0.7/x_4 + 0.3/x_5$ if x is A_1 and x is A_2 then x is $B = 1/x_1 + 1/x_2 + 1/x_3 + 1/x_4 + 1/x_5$ and is not
103 known Zadeh conditional inference is not suitable The fuzziness may be given for rule as If Depression is High
104 and Temperature is High and Wave velocity is High Then Coastal Erosion is Savior $= \min(1, (1 - \min\{0.6, 0.7, 0.8\}$
105 $+ 0.9)) = 1$ and is unknown Zadeh fuzzy conditional inference is not suitable when consequent part is unknown
106 Mamdani inference is given by if x_1 is A_1 and x_2 is A_2 and ? and x_n is A_n then y is $B = \min(A_1, A_2, \dots,$
107 $A_n, B)$ The proposed fuzzy conditional inference for Mamdani fuzzy inference is given as when the consequent
108 part is unknown $= \min(A_1, A_2, \dots, A_n, 1)$, where $B=1$ because B is not known. $= \min(A_1, A_2, \dots, A_n, 1)$
109 $= \min(A_1, A_2, \dots, A_n)$ if x_1, \dots, x_n then $y = f(x_1, x_2, \dots, x_n)$ is B

110 A method is possible to define with memberships of x_1, x_2, \dots, x_n when consequent part is not known

111 The proposed method for TSK fuzzy conditional inference may be defined as using t-norm [5] If x is A_1 and
112 A_2 and ?, and A_{n-1} or A_n then y is $B = f(A_1, A_2, \dots, A_n)$ If x is A_1 and A_2 or A_3 then y is $B = A_1 \cdot A_2$
113 $\vee A_3 \min(\max(\mu_{A_1}(x), \mu_{A_2}(x)), \mu_{A_3}(x))$ Where t-norm is $t(a \vee b) = \max(a, b)$ $t(a \cdot b) = \min(a, b)$

114 if x is A_1 and x is A_2 then x is $B = 0.2/x_1 + 0.6/x_2 + 0.9/x_3 + 0.6/x_4 + 0.2/x_5$ The fuzziness may
115 be given for rule as If Depression is High and Temperature is High and Wave velocity is High Then Coastal
116 Erosion is Savior $= \min(0.6, 0.7, 0.8) = 0.6$ It may be observed that the proposed methods of Mamdani and TK
117 conditional inferences are equal.

118 V.

119 10 Presentation of Fuzzy Set Type-2

120 The fuzzy set type-2 is a type of fuzzy set in which some additional degree of information is provided [6] Definition:
121 Given some universe of discourse X , a fuzzy set type-2 A of X is defined by its membership function

122 11 Global Journal of Computer Science and Technology

123 Volume XX Issue IV Version I 15 Year 2020 () $\mu_A(x)$ taking values on the unit interval $[0,1]$ i.e. $\mu_{\tilde{A}}(x) \in [0,1]$
124 $[0,1]$

125 Suppose X is a finite set. The fuzzy set A of X may be represented as $A = \mu_{\tilde{A}_1}(x_1)/\tilde{A}_1 + \mu_{\tilde{A}_2}(x_2)$
126 $/\tilde{A}_2 + \dots + \mu_{\tilde{A}_n}(x_n)/\tilde{A}_n$ Headache = { 0.4/mild, 0.6/moderate, 0.9/severe} John has "mild headache"
127 with fuzziness 0.4 The fuzzy set type-2 may be defined as Definition: The fuzzy set type-2 \tilde{A} is characterized by
128 membership function $\mu_{\tilde{A}}: X \times Y \rightarrow [0,1]$, $x \in X$ and $y \in Y$ Suppose X is a finite set. The fuzzy set A of X may be new
129 represented by $\tilde{A} = \mu_{\tilde{A}}(x,y)/x/y = \mu_{\tilde{A}}(x,y) = (\mu_{\tilde{A}}(x_1, y_1)/x_1 + \mu_{\tilde{A}}(x_2, y_1)/x_2 + \dots + \mu_{\tilde{A}}(x_n, y_1)/x_n)$
130 $/y_1 + (\mu_{\tilde{A}}(x_1, y_2)/x_1 + \mu_{\tilde{A}}(x_2, y_2)/x_2 + \dots + \mu_{\tilde{A}}(x_n, y_2)/x_n)/y_2 + \dots + (\mu_{\tilde{A}}(x_1, y_m)$
131 $/x_1 + \mu_{\tilde{A}}(x_2, y_m)/x_2 + \dots + \mu_{\tilde{A}}(x_n, y_1)/x_n)/y_m$ $\tilde{A} = \{ (0.1/x_1 + 0.2/x_2 + 0.3/x_3$
132 $+ 0.35/x_4 + 0.4/x_5)/high + (0.4/x_1 + 0.45/x_2 + 0.5/x_3 + 0.55/x_4 + 0.6/x_5)/normal + (0.7/x_1 + 0.75/x_2$
133 $+ 0.8/x_3 + 0.85/x_4 + 0.9/x_5)/low \}$ Let ? and ? be the fuzzy sets. The operations on fuzzy sets type-2 are
134 given as

135 12 Fuzzy Inference System

136 Fuzzy Inference System is Fuzzy Control System, which contains fuzzification and defuzzification. The Fuzzification
137 will be defined using the fuzzy rule. The fuzzy algorithm is a set of statements with a single fuzzy value. The
138 fuzzy conditional statement is defined as fuzzy algorithm if x_i is A_1 and x_i is A_2 and ? and x_i is A_n then
139 y is B The precedence part may contain and/or/not.

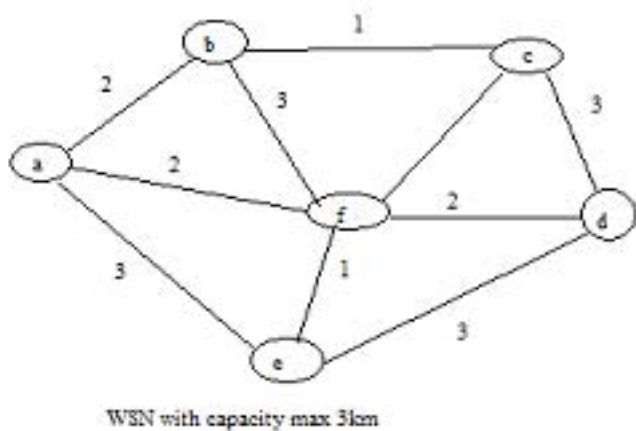
140 The Fuzzy Control System consists of a set of fuzzy rules If (set of conditions are satisfied then (set of
141 consequences inferred).

142 13 Conclusion

143 Some methods are studied for fuzzy conditional inference when prior information is unknown to consequent part.
144 Zadeh and Mamdani methods are not suitable when prior information is unknown. A new method is proposed
145 for "if ? then ?" when prior information is unknown to the consequent part with single fuzzy member function,
146 and two fuzzy membership functions. Fuzzy Certainty Factor is defined with two membership functions to make
147 a single fuzzy membership function. WSN are send data to the base station. The Fuzzy inference system (FIS)
148 is Studied for WSN to detect Coastal erosions. The Prim's algorithm is used to construct a spanning tree for
149 collection of Data from WSN to base station. Sensors are discussed an application for proposed fuzzy conditional
150 inference. The Fuzzy Control System is given an example for FCF. ^{1 2}

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3511

Figure 1: 3 /x 5 B 1 Fig. 1 :

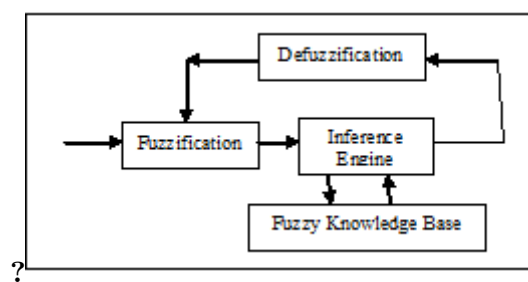


Figure 2: E T ? ?

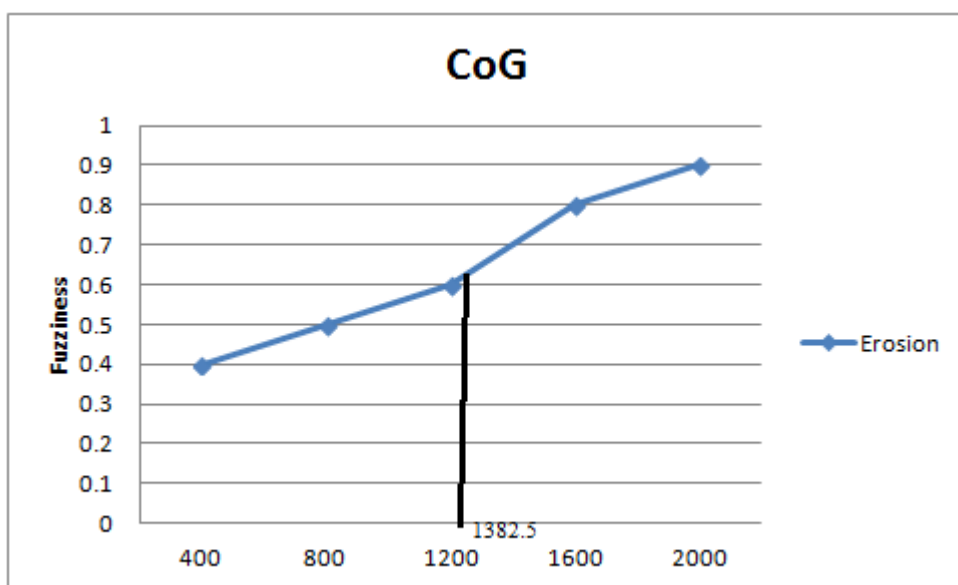


Figure 3:

151 .1 Acknowledgment

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153 [Mamdani and Assilian (1999)] ‘An Experiment in Linguistic Synthesis with a Fuzzy Logic Controller’. E H
154 Mamdani , S Assilian . *International Journal of Human-Computer Studies* August 1999. 62 (2) p. .

155 [Wang and Wang ()] ‘Design and Implementation of Intelligent Surge Controller for Modren Turbo Charged
156 Automobiles’. C H Wang , C Wang . *International Journal of Fuzzy Systems* 2014. 16 p. .

157 [Takagi and Sugeno ()] ‘Fuzzy Identification of Systems and Its application to Modeling and control’. T Takagi,
158 , M Sugeno . *IEEE Transactions on Systems Man and Cybernetics*, 1985. 15 p. .

159 [Sugeno and Kong ()] ‘Fuzzy Modeling and Control of Multilayer Incinerator’. M Sugeno , G Kong . *Journal of*
160 *Fuzzy Sets Systems* 1986. 18 (3) p. .

161 [Zadeh ()] ‘Fuzzy sets’. L Zadeh . *Information Control* 1965. 8 p. .

162 [Zadeh (ed.) ()] *Fuzzy sets and their applications to cognitive and decision processes*, L A Zadeh . L.A.Zadeh,
163 K.S.Fu, M.Shimura (ed.) 1975. New York, Academic. p. . (Calculus of Fuzzy restrictions)

164 [Venkata Subba and Reddy (2014)] ‘Generalization of Fuzzy Sets Type-2, Fuzzy Quantifiers Sets and ?-Cut
165 Fuzzy Sets Fuzzy Temporal Sets, Fuzzy Granular Sets and Fuzzy rough Sets for Incomplete Information’.
166 P Venkata Subba , Reddy . *International Conference on Fuzzy Theory and Its Applications*, (Kaohsiung)
167 2014. 2014. November 26-28, 2014.

168 [Venkata Subba and Reddy] ‘Generalized fuzzy logic for incomplete information’. P Venkata Subba , Reddy .
169 IEEE-FUZZ 2013. *IEEE International Conference on Fuzzy Systems*,

170 [Nanda and Kumar Rath ()] ‘Saroj Kuma Rout, Real Time Wireless Sensor Network for Coastal Erosion using
171 Fuzzy Inference System’. Arabinda Nanda , Amiya Kumar Rath . *International Journal of Computer Science*
172 *& Emerging Technologies (IJCSET)* 2010. 1 (2) p. .

173 [Flaminio and Marchioni ()] *T-Norm Based Logics with an Independent Involutive Negation, Fuzzy Sets and*
174 *Systems*, T Flaminio , E Marchioni . 2006. 157 p. .

175 [Venkata Subba and Reddy ()] P Venkata Subba , Reddy . *Fuzzy conditional inference for medical diagnosis,*
176 *International Conference on Fuzzy Theory and Technology Proceedings, Abstracts and Summaries*, 1993.