

Fuzzy Reinforcement Learning using Neural Network: An Application to Medical Diagnosis and Business Intelligence

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Received: 11 June 2021 Accepted: 1 July 2021 Published: 15 July 2021

Abstract

The information available to the system is incomplete in many applications, particularly in Decision Support Systems. The fuzzy logic deals incomplete information with belief rather than likelihood (probability). Sometimes the decision has to be taken with fuzzy information. In this paper, fuzzy machine learning is studied for decision support systems. The fuzzy Decision set is defined with two-fold fuzzy set. The fuzzy inference is studied with fuzzy neural network for fuzzy Decision sets. Business application is given as application.

Index terms— component, formatting, style, styling

1 Introduction

Information available to many applications like Business, Medical, Geological, Control Systems, etc is incomplete or uncertain. The fuzzy logic will deal with incomplete information with belief rather than likelihood (probable). Zadeh formulated uncertain information as fuzzy set with a single membership functions. The fuzzy set with two membership functions will give more evidence than a single membership function. The two-fold fuzzy set is with fuzzy membership functions "Belief" and "Disbelief". Usually, in Medical and Business applications, there are two opinions like "Belief" and "Disbelief" about the information and decision has to be taken under risk. For instance, in Mycin [1], the medical information is defined with belief and disbelief i.e.

$$2 \quad /, CF[h,e]=MB[h,e] -MD[h,e],$$

where "e" is the evidence for given hypothesis "h". The fuzzy set is used instead of Probability to define fuzzy certainty factor.

The fuzzy neural networks are one of the learning techniques to study fuzzy problems. In the following, some methods of fuzzy conditional inference are studied through fuzzy neural network and before that preliminaries of fuzzy logic and neural network are discussed.

In the following fuzzy logic [10] and Generalized fuzzy logic [9] are studied briefly. The fuzzy Certainty Factor is studied and fuzzy Decision set is proposed. The fuzzy inference and fuzzy reasoning are studied for fuzzy Decision set. The Business applications are studied as applications of fuzzy Decision set.

Author: e-mail: pvsreddy@hotmail.co.in II.

3 Fuzzy Logic

Various theories are studied to deal with imprecise, inconsistent and inexact information and these theories deal with likelihood whereas fuzzy logic with belief. Zadeh [10] has introduced fuzzy set as a model to deal with uncertain information as single membership functions. The fuzzy set is a class of objects with a continuum of grades of membership. The set A of X is characterized by its membership function $\mu_A(x)$ and ranging values in the unit interval For instance "Rama has mild headache" with Fuzziness 0.4[0, 1]. $\mu_A(x): X \rightarrow [0, 1], x \in X$,

The fuzzy logic is defined as combination of fuzzy sets using logical operators [11]. Some of the logical operations are given below Let A, B and C are fuzzy sets. The operations on fuzzy sets are Negation If x is not A $A' = 1 - \mu_A(x)$

4 Conjunction

x is A and y is B? (x, y) is A x B A x B = min(μ A (x), μ B (y))(x,y)

5 If x=y

x is A and y is B? (x, y) is A?B = min(μ A (x), μ B (y))/x x is A or y is B? (x, y) is A' x B' A' x B' = max(μ A (x), μ B (y))(x,y) If x=y x is A and x is B? (x, x) is A V B AVB = max(μ A (x), μ B (y))/x Disjunction Implication If x is A then y is B = A?B = min{1, 1-μ A (x) + μ B (y)}/(x,y) if x= y A?B = min {1, 1-μ A (x) + μ B (y)}/x If x is A then y is B else y is C = A x B + A' x C

The fuzzy proposition "If x is A then y is B else y is C" may be divided into two clause "If x is A then y is B" and "If x is not A then y is C"[15] If x is A then y is B else y is C = A?B = min {1, 1-μ A(x) + μ B(y)}/(x,y) If x is not A then y is B else y is C = A'? C = min {1, 1-μ A (x) + μ C (y)}/(x,y) Composition A o B = A x B = min{ μ A (x), μ B (y)}/(x,y) If x = y A o B = min{ μ A (x), μ B (y)}/x Composition

The fuzzy propositions may contain quantifiers like "Very", "More or Less". These fuzzy quantifiers may be eliminated as Concentration x is very A μ very A (x), = μ A (x) ²

6 Diffusion

x is very A μ more or less A (x) = μ A (x) 0.5

7 III. Generalized Fuzzy Logic with two-Fold Fuzzy Set

Since formation of the generalized fuzzy set simply as two-fold fuzzy set and is extension Zadeh fuzzy logic. The fuzzy logic is defined as combination of fuzzy sets using logical operators. Some of the logical operations are given below Suppose A, B and C are fuzzy sets. The operations on fuzzy sets are given below for two-fold fuzzy sets.

Since formation of the generalized fuzzy set simply as two-fold fuzzy set, Zadeh fuzzy logic is extended to these generalized fuzzy sets. Negation A? = {1-μ A Belief (x), 1-μ A Disbelief (x) }/x Disjunction AVB = { max(μ A Belief (x) , μ A Belief (y)) , max(μ B Disbelief (x) , μ B Disbelief (y)) }/x,y Conjunction A?B = { min(μ A Belief (x) , μ A Belief (y)) , min(μ B Disbelief (x) , μ B Disbelief (y)) }/x,y Implication A?B = {min (1, 1-μ A Belief (x) + μ B Belief (y)) , min (1, 1-μ A Disbelief (x) + μ B Disbelief (y)) }/x,y If x is A then y is B else y is C = A x B + A' x C If x is A then y is B else y is C = A?B = {min (1, 1-μ A Belief (x) + μ B Belief (y)) , min (1, 1-μ A Disbelief (x) + μ B Disbelief (y)) }/x,y if 'A If x is not A then y is B else y is C = A??C = min (1, μ A Belief (x) + μ C Belief (y)) , min (1, μ A Disbelief (x) + μ C Disbelief (y)) }/x,y Composition A o R = {min x (μ A Belief (x) , μ A Belief (x)) , min x (μ R Disbelief (x) , μ R Disbelief (x)) }/y

The fuzzy propositions may contain quantifiers like "very", "more or less". These fuzzy quantifiers may be eliminated as Concentration "x is very A μ very A (x) = { μ A Belief (x) ² , μ A Disbelief (x) μ A (x) ² }

Diffusion "x is more or less A" μ more or less A (x) = (μ A Belief (x) 0.5 , μ A Disbelief (x) μ A (x) 0.5

For instance, Let A, B and C are A = { 0.8/x 1 + 0.9/x 2 + 0.7/x 3 + 0.6/x 4 + 0.5/x 5 , 0.4/x 1 + 0.3/x 2 + 0.4/x 3 + 0.7/x 4 + 0.6/x 5 } B = { 0.9/x 1 + 0.7/x 2 + 0.8/x 3 + 0.5/x 4 + 0.6/x 5 , 0.4/x 1 + 0.5/x 2 + 0.6/x 3 + 0.5/x 4 + 0.7/x 5 } A V B = { 0.9/x 1 + 0.9/x 2 + 0.

8 Fuzzy Neural Network

The neural network concept is taken from the Biological activity of nervous system. The neurons passes information to other neurons. There are many models described for neural networks. The McCulloch-Pitts model contributed in understanding neural network and Zadeh explain that activity of neuron is fuzzy process [13].

The McCulloch and Pitt's model consist of set of inputs, processing unit and output and it is shown in Fig.

9 Fuzzy Decision Set

Zadeh [10] proposed fuzzy set to deal with incomplete information. Generalized fuzzy set with two-fold membership function μ A (x) = { μ A Belief (x) , μ A Disbelief (x) } is studied [18] The fuzzy Certainty Factor may be defined as (FCF) The Generalized fuzzy set for Demand for the Items and fuzzy certainty factor is shown in Fig5. Decision may be taken under Decision shown in Fig. ?? μ A FCF (x) = μ A Belief (x) - μ A Disbelief (x) , where μ A FCF (x) = μ A Belief (x) - μ A Disbelief (x) μ A Belief (x) ? μ A Disbelief (x) = 0 μ A Belief (x) < μ A Disbelief (x)

10 Fig. 6: Fuzzy Decision set

The fuzzy logic is combination of logical operators. Consider the logical operations on fuzzy Decision sets r1, R2 and R3 Negation If x is not R1 () D Year 2021 R1' = 1-μ R1 (x)/x Conjunction x is R1 and y is R2? (x, y) is R1 x R2 R1 x R2 = min(μ R1 (x), μ R2 (y))(x,y) If x=y x is R1 and y is R2? (x, y) is R1?R2 R1?R2 = min(μ R1 (x), μ R2 (y))/x x is R1 or y is R2? (x, y) is R1' x R2' R1' x R2' = max(μ R1 (x), μ R2 (y))(x,y) If x=y x is R1 and x is R2? (x, x) is R1 V R2 R1VR2 = max(μ R1 (x), μ R2 (y))/x Disjunction Implication if x is R1 then y is R2 = R1?R2 = min{1, 1-μ R1 (x) + μ R2 (y)}/(x,y) if x= y R1?R2 = min {1, 1-μ R1 (x) + μ R2 (y)}/x

98 Composition $R1 \circ R2 = R1 \times R2 = \min\{\mu_{R1}(x), \mu_{R2}(y)\} / (x,y)$ If $x = y$ $R1 \circ R2 = \min\{\mu_{R1}(x), \mu_{R2}(y)\} / x$
 99
 100 The fuzzy propositions may contain quantifiers like "Very", "More or Less". These fuzzy quantifiers may be
 101 eliminated as

11 Concentration

12 Fuzzy Conditional Inference in Decision Making

104 Decision management is usually happens in Decision Support Systems.

13 Conclusion

106 The decision has to be taken under incomplete information in many applications like Business, Medicine etc. The
 107 fuzzy logic is used to deal with incomplete information The fuzzy Decision set is defined with twofold fuzzy set.
 108 The fuzzy logic is discussed with two-fold fuzzy set. The fuzzy Decision set, inference and reasoning are studied.
 The Business applications is discussed for fuzzy Decision set. ^{1 2 3}

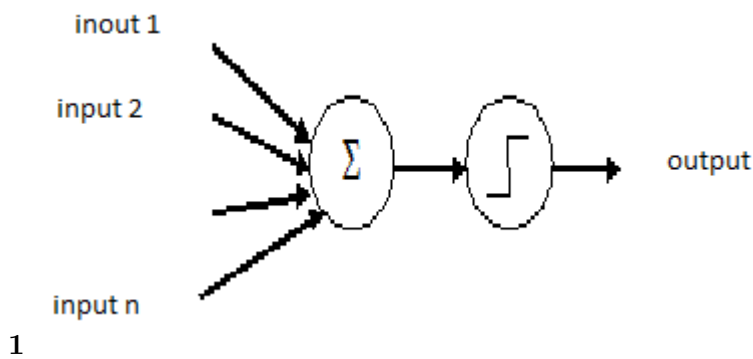


Figure 1: Fig. 1 :

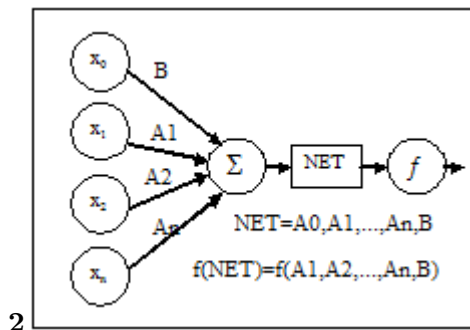


Figure 2: 2

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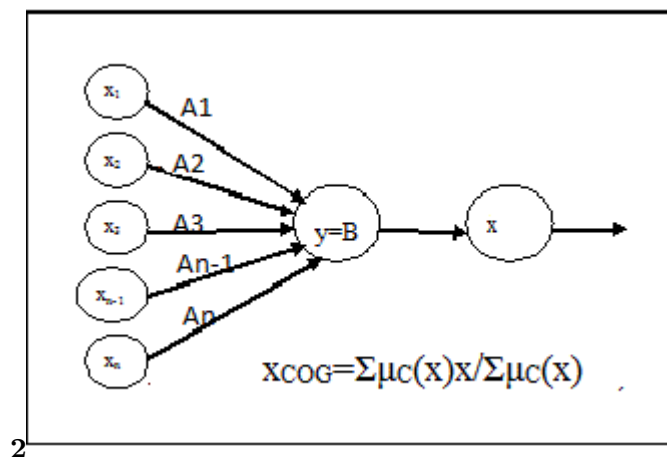


Figure 3: Fig. 2 :

2

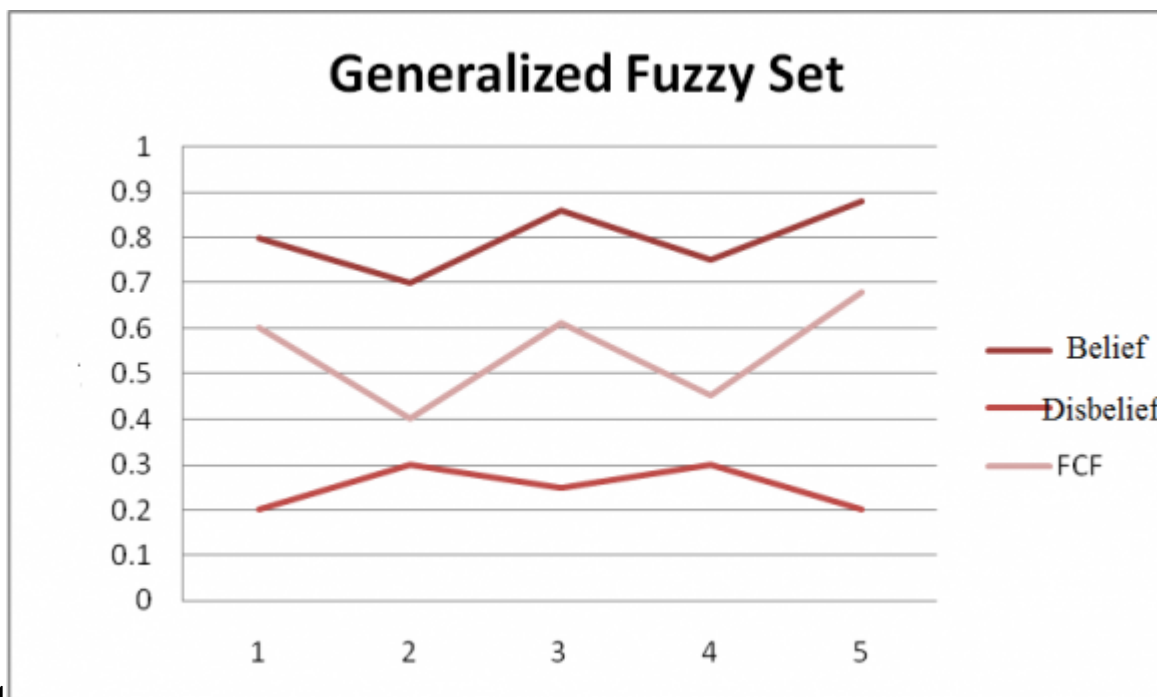


Figure 4: Fig. 3 : 4 Fig

34



Figure 5: Fuzzy

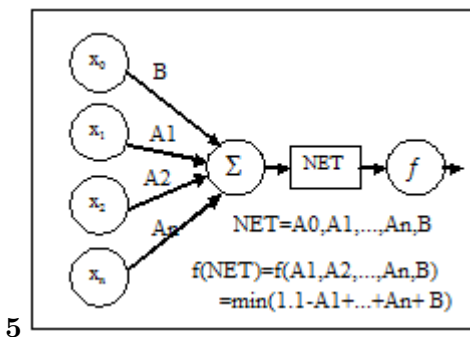


Figure 6: Fig. 5 :

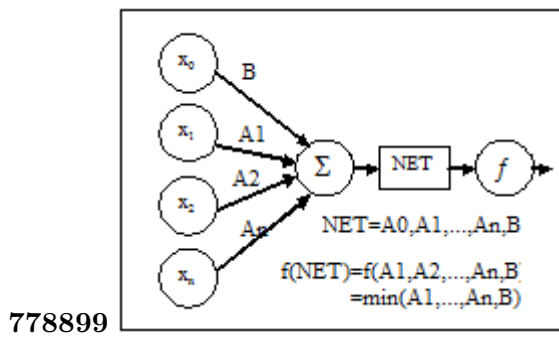


Figure 7: x 7 Fig. 7 : 8 Fig. 8 : 9 Fig. 9 :

Young={.95/10+0.9/20+0.8/30+0.6/40+0.4/50+0.3/60+0.2/70+0.15/80+0.1/90}

Not young={ 0.05/10 + 0.1/20 + 0.2/30+0.4/40 +0.6/50 + 0.8/60+0.7/70 +0.95/80+0.9/90 }

For instance "Rama is young" and the fuzziness of "young" is 0.8 The Graphical representation of young and not young is shown in fig.1

[Note: $A = \mu A(x_1)/x_1 + \mu A(x_2)/x_2 + \dots + \mu A(x_n)/x_n$, "+" is union For example, the fuzzy proposition "x is young"]

Figure 8:

μ More or Less A (x)

$$\begin{aligned}
 & 0.16/x_1 + 0.09/x_2 + 0.16/x_3 + 0.49/x_4 \\
 & = (\mu A \quad \text{Belief} \quad \text{Disbelief} \\
 & \quad (x) \quad (x) \mu \\
 & \quad 1/2 \quad A \\
 & \quad , \quad (x) \\
 & \quad \mu \quad 1/2 \\
 & \quad A \quad \} \\
 & = \{ 0IV.
 \end{aligned}$$

Year 2021

$$\{ 0.8/x_1 + 0.7/x_2 + 0.6/x_3 + 0.5/x_4 + 0.4/x_5 \} \quad A \quad ? \quad B = \{ 0.8/x_1 + 0.7/x_2 + 0.6/x_3 + 0.5/x_4 + 0.4/x_5 \}$$

[Note: $A(x) = \{ 0.64/x_1 + 0.81/x_2 + 0.49/x_3 + 0.36/x_4 + 0.25/x_5 \}$]

Figure 9:

Zadeh inference is given as $A \circ B = \min\{1, 1 - \mu_A(x) + \mu_B(x)\}$
 $\mu_{\text{Demand ? High Price}}$

$\mu_{\text{Demand ? High Price}}$

Mamdani inference is given as $A \circ B = \min\{\mu_A(x), \mu_B(x)\}$
 $\mu_{\text{Demand ? High Price}}$

$\mu_{\text{Demand ? High Price}}$

Mamdani inference is given as $A \circ B = \min\{\mu_A(x)\}$

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 Example 2

$\mu_{\text{Demand ? High Price}} \mu_{\text{Demand ? High Price}} \text{FCF}(x) = 0.4/x_1 + .44/x_2 + .44/x_3 + .44/x_4 + .44/x_5$

Consider Medical Diagnosis
 If x has infection in the leg then surgery
 Let x1, x2, x3, x4, x5 are the Patients.
 The fuzzy set

$$\begin{aligned} \mu_{\text{Infection}} \text{FCF}(x) &= 0.76/x_1 + 0.78/x_2 + 0.46/x_3 + 0.86/x_4 + 0.58/x_5, \\ &= 0.16/x_1 + 0.12/x_2 + 0.06/x_3 + 0.14/x_4 + 0.05/x_5 \\ \mu_{\text{Surgery}} \text{FCF}(x) &= 0.6/x_1 + 0.64/x_2 + 0.4/x_3 + 0.72/x_4 + 0.53/x_5 \\ &= 0.59/x_1 + 0.26/x_2 + 0.55/x_3 + 0.24/x_4 + 0.35/x_5, \\ &= 0.09/x_1 + 0.06/x_2 + 0.05/x_3 + 0.04/x_4 + 0.03/x_5 \\ &= 0.5/x_1 + 0.2/x_2 + 0.5/x_3 + 0.2/x_4 + 0.32/x_5 \end{aligned}$$

(Using inference rule $A \circ B = \min\{1, 1 - \mu_A(x) + \mu_B(x)\}$)
 D

$\mu_{\text{Infection ? Surgery}}$

$\mu_{\text{Infection ? Surgery}}$

$0 \mu_{\text{Infection ? Surgery}}$

The fuzzy risk set R is

$$1/x_1 + 0/x_2 + 1/x_3 + 1/x_4 + 1/x_5$$

Example 1

$\mu_{\text{Infection ? Surgery}}$

Consider Business rule

$\mu_{\text{very Surgery}}$

If x is Demand of the product then x is High Price Let x1, x2, x3, x4, x5 be the Items. x is very Demand
 The Generalized fuzzy set

$$= 0.35/x_1 + 0.66/x_2 + 0.35/x_3 + 0.04/x_4 + 0.1/x_5$$

Demand = { 0.56/x1+0.48/x2+0.86/x3+0.36/x4+0.88/x5, 0.06/x1+0.04/x2+0.07/x3+0.03/x4+0.2/x5 }
 VII. μ_{Demand}

High Price = 0.49/x1+0.52/x2+0.35/x3+0.4/x4+0.3/x5,

$$\begin{aligned} &= 0.09/x_1 + 0.02/x_2 + 0.06/x_3 + 0.02/x_4 + 0.1/x_5 \\ &= \mu_{\text{High Price}} \end{aligned}$$

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- 110 [Shafer and Mathematical ()] , G Shafer , Mathematical . 1976. Princeton, NJ: University Press.
- 111 [Mamdani and Assilian ()] ‘An experiment in linguistic synthesis with a fuzzy logic control’. E H Mamdani , S
112 Assilian . *International Journal of Man-Machine Studies* 1975. 7 (1) p. .
- 113 [Venkata Subba and Reddy ()] ‘Fuzzy Conditional Inference for Medical Diagnosis’. P Venkata Subba , Reddy
114 . *Proceedings of Second International Conference on Fuzzy Theory and Technology, Summary FT & T1993*,
115 (Second International Conference on Fuzzy Theory and Technology, Summary FT & T1993) 1993. p. .
- 116 [Zadeh] ‘Fuzzy Logic, Neural Networks and Soft Computing’. L A Zadeh . *Communications of ACM* 37 (3) p. .
- 117 [Venkata and Reddy ()] ‘Generalized fuzzy logic for Incomplete Information’. Poli Venkata , Subba Reddy . *IEEE*
118 *International Conference on fuzzy Systems*, (Hyderabad, India) July 7-10, 2013.
- 119 [Ren Ping ()] ‘Generalized fuzzy set s and Representation of Incomplete Knowledge’. Ren Ping . *fuzzy set s and*
120 *Systems*, 1990. 1 p. .
- 121 [Zadeh ()] *Generalized theory of uncertainty (GTU)-principal concepts and ideas Computational Statistics &*
122 *Data Analysis*, L A Zadeh . 2006. 51 p. .
- 123 [Zadeh (ed.) ()] *In fuzzy set s and their Applications to Cognitive and Decision Processes*, L Zadeh . L. A. Zadeh,
124 King-Sun FU, Kokichi Tanaka and Masamich Shimura (ed.) 1975. New York: Academic Press. p. . (Calculus
125 of fuzzy Restrictions)
- 126 [Pedrycz and Gomide ()] *Introduction to fuzzy set s*, W Pedrycz , F Gomide . 1998. Cambridge, MA: MIT Press.
- 127 [Rescher ()] *Many-Valued Logic*, N Rescher . 1969. New York: McGraw-Hill.
- 128 [Buchanan and Shortliffe ()] *Rule-Based Expert System: The MYCIN Experiments of the Stanford Heuristic*
129 *Programming Project, Readings*, B G Buchanan , E H Shortliffe . 1984. Addition-Wesley, M.A.
- 130 [Venkata et al. ()] ‘Some Methods of Reasoning for Conditional Propositions’. Poli Venkata , Subba Reddy , M.
131 Syam Babu . *fuzzy set s and Systems*, 1992. 52 p. .
- 132 [Zadeh ()] L A Zadeh . *fuzzy sets, In Control*, 1965. 8 p. .