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1 2	Crowd Behavior Analysis and Classification using Graph Theoretic Approach
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7 Abstract

Surveillance systems are commonly used for security and monitoring. The need to automate 8 these systems is well understood. To address this issue we introduce the Graph theoretic 9 approach based Crowd Behavior Analysis and Classification System (GCBACS). The crowd 10 behavior is observed based on the motion trajectories of the personnel in the crowd. Optical 11 flow methods are used to obtain the streak lines and path lines of the crowd personnel 12 trajectories. The streak flow is constructed based on the path and streak lines. The personnel 13 and their respective potential vectors obtained from the streak flows are used to represent 14 each frame as a graph. The frames of the surveillance videos are analyzed using graph 15 theoretic approaches. The cumulative variation in all the frames is computed and a threshold 16 based mechanism is used for classification and activity recognition. The experimental results 17 discussed in the paper prove the efficiency and robustness of the proposed GCBACS for crowd 18 behavior analysis and classification. 19

20

Index terms— video surveillance, crowd motion, crowd behavior, optical flow, streak lines, path lines, streak line flow, graph theory, threshold, abnormal, normal,

23 1 Introduction

ideo surveillance systems fed by multiple high definition video streams have become a common feature in public and private spaces. The video surveillance systems are generally used to monitor activities and maintain vigil. The steady population growth observed in the past decade have resulted large crowd movements especially in public spaces like airports, train stations, bus stations, shopping malls, religious places, etc. The video surveillance feeds of such public spaces are currently monitored manually and are prone to human error. The number of crowd accidents observed have increased in the recent times [1].

The need for automated systems to classify the movements of crowds or detect abnormal activity can be 30 considered as an open research issue. A crowd can be considered as a collection of people distributed over the 31 region of interest. Tracking of human activity or personnel counting within video surveillance systems has been 32 researched upon [2] [3] [4] for some time now. The open research issues that exist and require attention with 33 34 respect to crowd analysis can be listed as modelling or knowledge extraction from crowd patterns [5][6] [7] [8] 35 and crowd behavior analysis [9] [10] [11]. Limited work is carried out to classify the behavior of crowds in 36 surveillance systems. The research work presented in this paper introduces the Graph theoretic approach based Crowd Behavior Analysis and Classification System (?????????). To achieve accurate classification results 37 the behavior of the personnel in the crowd needs to be analyzed first. The behavior of the personnel in the 38 crowd can be analyzed based on the motion or trajectory activities observed. Based on the behavior of the 39 personnel analyzed, it can be classified into normal or abnormal activity. Abnormal activity detection is achieved 40 by observing unusual behavior of personnel or group of personnel within a crowd. Activities like instantaneous 41 disbursement, sudden convergence or fighting are classified as abnormal activities. 42

To study the behavior of personnel in the crowd, tracking methodologies are generally used. The commonly 43 used tracking methodologies [2] [3] [4] fail when large crowds are considered. To overcome this drawback, 44 researchers proposed the consideration of fixed cell sizes to identify local trajectories and later map it together to 45 obtain the personnel trajectory patterns [8] [10] [12]. The frames are split into uniform cells in these approaches. 46 The use of optical flow techniques within each cell is considered to obtain the trajectory patterns of personnel 47 within a cell. The optical flow techniques exhibited better results when compared to traditional tracking 48 methodologies [13]. The drawback of the optical flow is that only two consecutive frames are considered to 49 obtain personnel trajectory patterns. The optical flow method are not able to capture long term does temporal 50 dependencies [14]. To overcome this drawback the concept of particle flow was introduced in [14]. The particle 51 flow computation is achieved by displacing a grid of particles with optical flow through numerical integration 52 techniques, providing trajectories that relate a particles original position to its position at a later time. The 53 particle flow mechanisms proved to be computationally very heavy and minute personnel motion details were 54 ignored. The introduction of streaklines flows to obtain the trajectories of personnel in the crowd proved to 55 provide accurate analysis results [15]. For crowd behavior classification in [16] an unsupervised machine learning 56 technique based framework was proposed. The framework in [16] considered hierarchical Bayesian models to 57 58 connect the visual features, "atomic" activities and the interactions for classification. In [15] streaklines coupled 59 with social force models were used to detect abnormal activities.

60 The work carried out so far by researchers, primarily concentrates on analysis of activities amongst a few 61 personnel present in the crowd only, and do not take into account the inter personnel activities for classification. To overcome this drawback the ????????? presented in this paper considers inter personnel activities for 62 analysis. The inter personnel activities are monitored through the motion vectors observed. To obtain the 63 behavioral vectors of personnel in the crowd video an optical flow is initially computed. Based on the optical 64 flow the path lines and streak lines are obtained. The path lines, streak lines are used to derive the streak flow 65 vectors which define the potential and personnel flow. Every frame of the video is analyzed using graph theoretic 66 approaches. The ????????? considers each frame as a graph with sub graphs. All the frames are analyzed 67 and the cumulative variance is computed. If the ????????? observes that the cumulative variance is greater 68 than a threshold the activity of the personnel in the crowd is classified as an abnormal activity. 69

74 **2** II.

75 **3** Literature Review

76 In this section of the paper a brief of the literature review conducted during the course of the research work 77 presented here is discussed.

Hang Su et al. [17] propose a novel spatiotemporal viscous fluid field to recognize the large-scale crowd behavior from both the appearance and driven factor perspectives and present a spatio-temporal variation matrix to capture crowd motion characteristics and model the motion pattern as a spatio-temporal variation fluid field. They construct a codebook by clustering neighboring pixels with similar spatiotemporal features, and consequently, crowd behaviors are recognized using the latent Dirichlet allocation model. The drawbacks of this paper, when the interaction among pedestrian and estimate the interaction force between the pedestrians with sheering force in viscous fluid, which is referred to as spatiotemporal force field.

Si Wu et al. [18] proposed approach which is based on optical flow. For low quality videos, the resulting optical flow fields become unstable. To reduce the impact of noise, we use a regular grid to partition the flow field into a set of patches and focus on the average optical flow vector of each patch. The drawback of the proposed approach is limited by the accuracy of optical flow estimation.

BerkanSolmaz et al [19] proposed a framework to identify multiple crowd behaviors (bottlenecks, fountainheads, lanes, arches, and blocking) through stability analysis for dynamical systems, without the need for object detection, tracking, or training. The proposed method is deterministic and cannot capture the randomness inherent in the problem without a stochastic component.

Duan-Yu Chen et al. [20] proposed a real time constraint, each isolated region is considered a vertex and a human crowd is thus modeled by a graph. To regularly construct a graph, Delaunay triangulation is used to systematically connect vertices and therefore the problem of event detection of human crowds is formulated as measuring the topology variation of consecutive graphs in temporal order.

NuriaPelechano et al. [21] have shown a significant improvement in evacuation rates when using inter-agent communication. We can also observe the grouping behavior that emerges when there are a high percentage of dependent agents in the crowd. Only a relatively small percentage of trained leaders yield the best evacuation rates. We can visualize these results in real time with either our simple 2D or 3D viewer. Areas where there is room for improvement include adding individualism into Helbing's model so that agents would have different local motions depending on their roles.

103 **4 III.**

¹⁰⁴ 5 Graph Theoretic Approach Based

105 Crowd Behavior Analysis and Classification System (GCBACS)a) System Modeling

Let us consider a surveillance video $?? \times ??$. The video represents a set of ?? frames and the dimension of 106 each image ?? is ?? × ?? pixels. Let us consider a frame ?? at the ?? ??? time instance and ?? ? ??. Similarly 107 the frame at the (?? + 1) ??? time instance is represented as ?? . The frame ?? 1 ? ?? is split into a number 108 of blocks and a mesh based structure is created for computational ease. Let the set I? J 2 represent the crowd 109 personnel to be observed in the surveillance video spaceJ 2. The set ?? consists of ?? personnel. The trajectory 110 of the ?? ??? personnel i.e. ?? ? ?? at the time instance ?? ?an be represented as ?? (??: ?? ??, ?? ???). 111 At the initial instance i.e. ?? ?= 0 the trajectory is represented as ?? (??: ?? 0, ?? 0). The trajectories is 112 utilized for optical computations. From the optical flows the streak lines ?? and path lines ?? of the personnel in 113 the crowd are computed frame wise. The streak flow?" is then derived which is used for analysis. For analysis a 114 115 analysis is carried out on the similarity and deviations are observed. Cumulative variance ∂ ?"½ ∂ ?"½?????? is 116 computed considering all the previous frames and the current frame. If the variance is greater than the threshold 117 ?? then abnormal activity is said to be detected. The ?????????? proposed in this paper can be understood 118 based on the model shown in Figure 1 of this paper. ?(??, ??) ?? ([?? ?? ? ð ??"ð ??" ?? ? 1, ?? ?? + ð ??"ð ??" 119 $?? + 1] \times [?? ?? ? \delta ??" \delta ??"?? ? 1, ?? ?? + \delta ??" \delta ??"?? + 1]), ??(??, ??) = ?? ?? (??, ??)(1)?(??, ??)??([??, ??)))$ 120 121 ?? ?? $(?? + \delta ??"\delta ??" ?? ?? , ?? + \delta ??"\delta ??" ?? ??)(2)$ 122

Where $\eth ??"\eth ??" ?? , \eth ??"\eth ??" ?? are two integer values and ?? and ?? represent the previous two$ frames. Based on the above equations it can be observed that there exist a domain definition difference between??(??, ??)and ??(??, ??). The optical flow representation of the frame ??(??, ??) is defined over the windowsize(2ð ??"ð ??" ?? + 3) × (2ð ??"ð ??" ?? + 3) instead of using (2ð ??"ð ??" ?? + 1) × (2ð ??"ð ??" ?? + 1).Consider that the displacement vector is?? ? = [?? ?? ?? ??] ?? = ?? ?? and image position vector is ?? =[?? ?? ?? ??] ?? The vector?? ? minimizes the matching function ??(?? ?

An iterative Lucas -Kanade method is adopted to solve the function ??(?? ?

) and is represented as ????(???) ?????? = ?????(??(+ð??"ð??"??)](6)

The derivative at [?? ??] ?? is defined as????(??, ??) = ??(??, ??) ? ??(??, ??)(7)

In Equation ??, ? ???? ???? ???? ???? ?is the gradient vector and ??? can be defined as???? = ? ?? ?? ??? 136 ?? ? = ? ???? ???? ???? ???? ??(8)

The derivatives ?? ?? and ?? ?? can be computed directly from the image ??(??, ??) in the $(2\delta$??" δ ??" ?? + 1) × $(2\delta$??" δ ??" ?? + 1), which is a neighborhood of the point ?? independently from the next image ??(??,

139 ??).

Based on ?? ?? (??, ??) and ?? ?? (??, ??) defined above the computation of???? (?? ?)

and matrix ?? is invertible, then the optical flow vector?? ? ?????? is defined as?? ? ?????? = ?? ?1 ???(14) Considering?? ? ?????? , it is evident that ?? (??, ??)contains information of the gradients in the ?? and ?? direction of ??. A large number of iterations have to be considered to obtain accurate optical flow of personnel in the crowd video frames. Let ?? represent the number of iterations required and ?? ? 1. Based on the optical flow computations from 1,2,3, ? (?? ? 1) the initial guess ?? ? ???1 for pixel displacement ?? ? is obtained. The initial guess is given as??? ???1 = [?? ?? ???1 ?? ????1] ?? .

If?? ?? represents the new image based on??? ???1, provided ?(??, ??) ?? [?? ?? ? δ ??" δ ??" ?? , ?? ?? + δ ??" δ ??" ??] × [?? ?? ? δ ??" δ ??" ?? , ?? ?? + δ ??" δ ??" ??] then ?? ?? (??, ??) = ??(?? + ?? ?? ???1 , 158 ?? + ?? ?? ???1)(15)

7 D) GRAPH THEROTIC MECHANISM FOR ANALYSIS AND CLASSIFICATION

In Equation 16???? ?? represents the ?? ??? frame difference and is defined as???? ?? (??, ??) = ??(??, ??) (??, ??) (19)

From Equation 18, we can observe that the spatial derivatives ?? ?? and ?? ?? are computed only once initially and ?? is constant for an entire iteration loop. The parameter vector ?? ?? ????is iteratively computed at ?? steps. That vector ?? ?? ???? is the amount of residual difference between the video frames after translation by the vector?? ? ????1. Based on the matrix ?? and?? ?? ????, ? ?? is computed.The new pixel displacement is ?? ???? that is computed in the step ?? + 1and is defined as?? ??? = ?? ????1 + ?? ??(20)

The optical flow based on the velocities in the ?? and ?? direction at the?? ??? time instance can be represented as?? ? = [?? ?? ?? ?? ??] ??(22)

¹⁷⁶ 6 c) Streakline Flow Computation

Where ?? ?? , ?? ?? are obtained from the optical flow vectors. For all the frames ?? and time ?? = 1,2,3 ? 179 ?? using particle advection we can obtain a vector matrix. The columns of the matrix can be used to obtain the 180 particle trajectory details from time ?? to the current time ?? and are called path lines. In this paper ? ?? (??, 181 ??) is used to represent the path lines. The row of the matrix can be used to obtain the streaklines that connect 182 the particles from ?? video frames that originated from the position ??. The streaklines is represented using? ?? 183 (0, ??) notation in this paper. Inconstancies are noticed in the streak lines obtained. To overcome this drawback 184 in [15] the extended particle was introduced based on the position ?? and the optical flow velocities. The?? ??? 185 extended particle can be defined as? ?? = ??? ?? ??? (??), ?? ?? ?? (??), ?? ?? ?? ?? ?? ?? ?? ?? (25) 186

Where?? ?? ?? = ?? ?? (?? ?? ?? (??), ?? ?? ?? (??), ??)and?? ?? ?? = ?? ?? (?? ?? ?? (??), ?? ?? ?? (??), ??). Based on the streak lines the behavior of the personnel in obtained. Using the streak lines, the streak flow is computed and is defined asÎ?" ?? = (?? ?? ?? , ?? ?? ??) ?? (26)

In Equation ??6?? ??????? represents the index of the pixel, ?? ð ??"ð ??"?? represents the basis function. Using the interpolation method the parameters ?? ?? ?? (?? 1), ?? ?? ?? (?? 2) and ?? ?? ?? (?? 3) are obtained. For all the vectors in ?? ?? and based on Equation 26 we can stated ?" ð ?" ?? ?? ?? ?? ?? ?? (28) Where ?? ð ??"ð ??"?? are the elements of the matrix ð ?" ð ?" . Based on Equation 25 and 26 similarly ?? ?? ?? can be computed. Using ?? ?? ?? and ?? ?? ?? the streak flow Î?" ?? is obtained. In ?????????????????? the use of streak flow to observe the trajectory of the personnel in the crowd is considered as the streak flow methodology enables instantaneous change observation when compared to particle flows.

²⁰³ 7 d) Graph Therotic Mechanism For Analysis And Classifica-²⁰⁴ tion

In ??????????? the behavior of crowd personnel observed using the streak flow is analyzed using a graph structure adopted for all the ?? frames of the video. Let us consider a graph \eth ?"³/4 \circlearrowright ?"⁴/4 \circlearrowright ?"⁴/4</sup>/4 \circlearrowright ??⁴/4</sup>/4 \circlearrowright ??⁴/4</sup>/4⁴/4</sup>/4 \circlearrowright ??⁴/4</sup>/4⁴/4</sup>/4⁴/4</sup>/4⁴/4</sup>/4⁴/4</sup>/4⁴/4</sup>/4⁴/4</sup>/4⁴/4</sup>/4⁴/4</sup>/4⁴/4</sup>/4⁴/4</sup>/4⁴/4⁴/4</sup>/4⁴/4⁴/4</sup>/4⁴/

The edges of the graph δ ?"³/4 δ ?"³/4 can be represented as δ ?"¹/4 δ ?"¹/4 = {? 1, ? 2, ? ?? ?? }(**30**)

The streak flow $\hat{1}$?" computed represents a planar field, and $\hat{1}$?" = $\hat{1}$?" ?? + $\hat{1}$?" ?? based on the decomposition defined by Helmholtz. $\hat{1}$?" ?? is the incompressible part and $\hat{1}$?" ?? is the irrotational part of the vector field. In [22] two functions are introduced such that, $\hat{1}$?" ?? = $\hat{1}$?"?? and $\hat{1}$?" ?? = $\hat{1}$?"??. The stream function ?? and the velocity potential function ?? are computed using Fourier Transforms as described in [22]. The functions ?? and ?? are defined as??(??, ??) = ?? 0 + ? 1 2 × ???? ?? ?? (??, ??) + ?? ?? ?? (0, ??)????? ?? 0 ? ? ? 1 2 × ???? ?? ?? ?? (??, ??) + ?? ?? ?? (??, 0)????? ?? 0 ?(**31**)??(??, ??) = ?? 0 + ? 1 2 × ???? ?? (??, ??) + ?? 216 ?? ?? (??, 0)????? ?? 0 ? + ? 1 2 × ???? ?? (??, ??) + ?? ?? (0, ??)????? ?? 0 ?(**32**)

The function ?? provides details of the steady motion vectors and ?? provides the details of the random motion changes detected. By combining the ?? and ?? vectors the potential functions of the video frame is computed and the edge set ∂ ?"¹/₄ ∂ ?"¹/₄ can be defined as ∂ ?"¹/₄ ∂ ?"¹/₄ = {?? , ??}(33)

To detect abnormal behavior analysis of consecutive frames is considered i.e. graph δ ?"³/₄ δ ?"³/₄???1 and graph δ ?"³/₄ δ ?"³/₄?? . The relation amongst the graphs can also be considered as the relation amongst the sub sets of δ ?"³/₄ δ ?"³/₄??1 and δ ?"³/₄ δ ?"³/₄?? and is defined as? δ ?"³/₄ δ ?"³/₄ ? ???1 , ?? ??) ?(**34**) 223 Where ? represents the number of vectors common to the graphs \eth ?"³4 \eth ?"³4 \circlearrowright ???¹1 (??, \eth ?"¹4 \eth ?"¹4 \circlearrowright)and 224 \eth ?"³4 \eth ?"³4 \circlearrowright ?"³4 \circlearrowright ?"¹4 \circlearrowright ?"¹4 \circlearrowright ?"¹4 \circlearrowright).?? \eth ?"³4 \eth ?"³4 \circlearrowright ?

226 IV.

227 8 Performance Evaluation

228 Minnesota ??23]. The dataset [23] consists of abnormal and normal crowd personnel videos. In this paper two 229 scenarios are from the dataset are considered. They are referred as scenario 1 and scenario 2 in this section of 230 the paper. The performance of the ?????????? is compared with the Viscous Fluid Field (?????) method 231 proposed in [17]. Matlab is used to develop ????????? . The performance presented here is based on the 232 recognition results and the quantitative evaluations studied. In scenario 1 the outdoor crowd personnel activity 233 is monitored. Indoor environments are characterized by lower lighting conditions and analyzing the personnel 234 behavior can be achieved only if robust techniques are in place. 235

²³⁶ 9 a) Recognition Results

237 and Scenario is shown in Figure ??. In the figure the use of bars is considered to represent the results where the 238 green bars represent normal crowd activity and the red bars represent abnormal crowd activity. From the figure 239 it is clear the proposed ?????????? exhibits better accuracy when compared to the system proposed in [17] i.e. 240 ?????? . The ??????????? nearly follows the ground truth bar shown in the figure. The misclassification ratio 241 of the ?????????? was found to be 0.05 and the miss classification ratio of ?????? was found to be 0.14. From 242 243 the figure it is noticed that the ?????? has a few misclassified values which is also seen in the results shown in [17]. The misclassification is reduced as the ?????????? adopts the streak line flow to capture the behavior 244 of personnel in the scenario videos considered. Based on the results it can be concluded that the ?????????? 245 proposed in this paper can be efficiently adopted for crowd behavior study and analysis under varying conditions 246 i.e. indoor and outside scenarios. 247

²⁴⁸ 10 b) Quantitative Evaluations

249 are considered to be positive events. The results are evaluated using receiver operating characteristic curves 250 (?????) [24]. The ?????? curve obtained for scenario 1, scenario 2 is shown in Figure 3 and Figure ??. From 251 Figure ?? and Figure ?? it is clear that the ?????????? exhibits a better crowd activity classification when 252 compared to the ?????? system. Considering Scenario 1 it is observed that the area under the ?????? curve for 253 254 255 scenario 2 is considered as the motion of the personnel in this video is relatively uniform. The motion trajectories 256 of personnel in scenario 1 is erratic and random. In both the scenarios the area under the ?????? curve of 257 258

The accuracy and efficiency plots for scenario 1 are shown in Figure ?? and Figure ?? of the paper. From 259 Figure ?? it is observed that average activity classification accuracy of ?????????????? is 0.83. The average activity 260 classification accuracy considering the ?????? system is 0.71. In Figure ?? it is observed that the crowd activity 261 classification efficiency of ????????? is 17.4% better than ?????? . Considering scenario 2 the crowd activity 262 classification accuracy and efficiency plots are shown in Figure 7 and Figure ?? Where ? is the number of matched 263 sub graphs observed in the graph frames ∂ ?"³/₄ ??³/₄ ??³/₄ ∂ ?"⁴/₄ ∂ ?"⁴/₄ ∂ ?"³/₄ ∂ ?"³/₄ ??³/₄ ??³/₄ ??³/₄ ? 264). ð ?"¾
ð ?"¾ ???1 ?????? represents the sub sets of ð ?"¾
ð ?"¾ ???1 andð ?"¾
ð ?"¾ ?? ?????? represents the 265 sub sets of ∂ ?"³4 ∂ ? 266 267

Where δ ??" δ ??"(??) is a function that defines the matching between the sub sets δ ?" δ ?

Where ?? is a predefined integer. The cumulative variance observed till the ?? ??? frame can be defined asð ?" $\frac{1}{20}$ asð ?" $\frac{1}{20}$?" $\frac{1}{2$

If the value of the cumulative variance is greater than a predefined threshold ?? then abnormal event is detected in the video and it is assigned the class 1 else 0. The classification can be defined as? ?? ????????? = $0, ??\delta ??"\delta ??"\delta ??"'\delta ??"'\delta ??"'\delta ??"'\delta ??''(40)$

Having discussed the ?????????? proposed in this paper, its performance is evaluated in the next section of this paper. accuracy of ?????????? is 0.88. The average activity classification accuracy of ?????? is 0.76.

11 CONCLUSION AND FUTURE WORK

287 11 Conclusion and Future Work

This paper introduces the ?????????? for surveillance video crowd behavior and analysis. The ?????????? 288 considers the use of streak flows to attain the crowd personnel behavior. The streak flows are obtained from the 289 streak lines and path lines. Optical flow methods are used to obtain the streak lines. The potential field variations 290 captured by the streak flows are analyzed using graph theoretic approaches. A threshold based scheme is adopted 291 to classify the cumulative variation observed in all the frames of the video. The crowd activity is classified as 292 normal and abnormal behavior based on the inter personnel activity. The experimental results presented in 293 this paper validate that the proposed ?????????? can be utilized for analysis of indoor and outdoor crowd 294 surveillance videos. The results validate that the proposed ????????? outperforms the existing methods used 295 for crowd behavior analysis and classification. The future of the research work presented in this paper is to 296



Figure 1: v

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Figure 2: Crowd



Figure 3: Figure 1 :



Figure 4:



Figure 5: 2 ? (9)

Figure 6:

10

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