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# <sup>1</sup> Statistical Modelling and Prediction of Rainfall Time Series Data

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#### 6 Abstract

Climate and rainfall are highly non-linear and complicated phenomena, which require classical, 7 modern and detailed models to obtain accurate prediction. In order to attain precise forecast, 8 a modern method termed fuzzy time series that belongs to the first order and time-variant 9 method was used to analyse rainfall since it has become an attractive alternative to traditional 10 and non-parametric statistical methods. In this paper, we present tools for modelling and 11 predicting the behavioural pattern in rainfall phenomena based on past observations. The 12 paper introduces three fundamentally different approaches for designing a model, the 13 statistical method based on autoregressive integrated moving average (ARIMA), the emerging 14 fuzzy time series (FST) model and the non-parametric method (Theil?s regression). In order to 15 evaluate the prediction efficiency, we made use of 31 years of annual rainfall data from year 16 1982 to 2012 of Ibadan South West, Nigeria. The fuzzy time series model has it universe of 17 discourse divided into 13 intervals and the interval with the largest number of rainfall data is 18 divided into 4 sub-intervals of equal length. Three rules were used to determine if the forecast 19 value under FST is upward 0.75â??"point, middle or downward 0.25-point. ARIMA (1, 2, 1) 20 was used to derive the weights and the regression coefficients, while the theil?s regression was 21 used to fit a linear model. The performance of the model was evaluated using mean squared 22 forecast error (MAE), root mean square forecast error (RMSE) and Coefficient of 23 determination (. The study reveals that FTS model can be used as an appropriate forecasting 24 tool to predict the rainfall, since it outperforms the ARIMA and Theil?s models. 25

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Index terms— fuzzy time series, autoregressive integrated moving average, theil?s regression, mean squared
 forecast error, root mean square forecast error and co

### <sup>29</sup> 1 Introduction

limate change seems to be the foremost global challenge facing humans at the moment, even though it seems that
not all places on the globe are affected. World leaders, union leaders, pressure groups and others who have shown
concern have been meeting to find a lasting solution to the 'acclaimed' dilemma. The scientific community has
not been left out as causes and solutions are being proffered and it is expected to linger on for a long time. One
of the indicators of climate change is rainfall (Adger et al., 2003;Frich et al., 2002; ??ovotny and Stefan, 2007).

Rainfall is a climate parameter that affects the way and manner men lives. It affects every facet of the ecological
system, flora and fauna inclusive. Hence, the study of rainfall is important and cannot be over emphasized (Obot
and Onyeukwu, 2010). Aside the beneficial aspect of rainfall, it can also be destructive in nature; natural disasters
like floods and landslides are caused by rain (Ratnayake and Herath, 2005).

Globally, lots of studies have been carried out on rainfall. A few of them is discussed briefly; Jayawardene et al. ??2005) observed different trends across Sri Lanka using 100 years data. Some parts recorded decreasing trend, some increasing trend while some locations showed no coherent trend. They also showed that the trend characteristics vary with the duration of the data analyzed. Smadi and Zghoul (2006) examined the trend analysis 43 of rainfall over Jordan picking three close-by locations. Their study covered a period of 81 years . Although, 44 different trends for different seasons across the three stations were observed, however, one of the stations showed 45 a decline in both the rainy days and the total amount of rainfall after the mid 1950s. While in Turkey, Partal and 46 Kahya (2006) examined the trend within a 64 year period of rainfall for 96 stations. The overall result indicated 47 that the trend in precipitation is downward, nonetheless, there are few stations that showed increasing trend.

Acknowledging some of the research that has been done, it is very important to discuss climatic changes as it has contributed to the instability of rainfall in Nigeria, then it becomes a very important and sensitive issue which requires adequate attention from governments, corporate organisations and researchers. Since climate and rainfall are highly non-linear and complicated phenomena, which require serious and vivid investigation and analysis. Then, this research is centred on analysing the pattern and structure of rainfall over 30 years in South West, Nigeria. Hence forecast values will be obtained in order to plan for the future.

In order to achieve our set objectives, classical, non-parametric and modern methods of discussing relationship and forecasting will be discussed. For classical forecasting method, we will consider autoregressive integrated moving average (ARIMA) which is a concept of autoregressive moving average while theil's regression will be used in the concept of non-parametric, where fuzzy time series method will be used in the concept of modern forecasting method. ARIMA is basically a linear statistical technique and has been quite popular for modeling the time series and rainfall forecasting due to ease in its development and implementation.

60 In contrast, fuzzy time series is another important modern forecasting method introduced by Song and Chissom 61 in 1993 and it is believed that the theory of fuzzy time series overcome the drawback of the classical time series methods, it has the advantage of reducing the calculation time and simplifying the calculation process. Based 62 on the theory of fuzzy time series, Song et al. presented some forecasting methods [Song (2003); and Song and 63 Leland (1996)] and these methods are now being used in several fields to obtain meaningful results. Furthermore, 64 theil's regression is a simple, non-parametric approach to fit a straight line to set of two points. This method 65 was introduced by Theil Sen in 1950 and it is has the ability to fit a linear trend when no assumptions about the 66 population distribution from which the data taken are known. 67

However, the three models will be used to forecast values for rainfall behaviour and the results will be compared to determine maybe the result obtained using classical forecasting method will better the result obtained for the non parametric and modern methods and vice verse.

#### 71 **2 II.**

#### 72 **3** Theory and Methods

#### <sup>73</sup> 4 a) Data Exploration

The pattern and general behaviour of the series is examined from the time plot. The series will be examined for stationarity, outliers and gaussianity. Test for stationarity will be carried out using correlogram.

76 Details of the test procedures can be found in Box and Jenkins (1976).

### 77 5 b) ARIMA Theory

ARIMA (autoregressive integrated moving average) models are generalizations of the simple AR model that use
three tools for modeling the serial correlation in the disturbance. The first tool is the autoregressive, or AR,
term. The ????(1) model use only the first-order term, but in general, you may use additional, higher-order AR
terms. Each AR term corresponds to the use of a lagged value of the residual in the forecasting equation for the
unconditional residual. An autoregressive model of order (??), ????(??) has the form:?? ?? = ?? 1 ?? ???1 +
?? 2 ?? ???2 + ? + ?? ?? ?? ????? + ?? ??

The second tool is the integration order term. Each integration order corresponds to differencing the series being forecast. A first-order integrated component means that the forecasting model is designed for the first difference of the original series. A second -order component corresponds to using second differences, and so on.

The third tool is the MA, or moving average term. A moving average forecasting model uses lagged values of the forecast error to improve the current forecast. A first order moving average term uses the most recent forecast error; a second-order term uses the forecast error from the two most recent periods, and so on. An MA(q

90 ) has the form:?? ?? = ?? ?? + ?? 1 ?? ???1 + ?? 2 ?? ???2 + ? + ?? ?? ?? ?????

The autoregressive and moving average specifications can be combined to form an ARMA (p, q) specification:?? ?? = ?? 1 ?? ???1 + ?? 2 ?? ???2 + ? + ?? ?? ?? ????? + ?? ?? ???1 + ?? 2 ?? ???2 + ? + ?? ?? ?? ????? i. Principles of ARIMA Modeling

In ARIMA forecasting, you assemble a complete forecasting model by using combinations of the three building blocks to be described below. The first step is forming an ARIMA model for a series of residuals by looking into its autocorrelation properties. We will make use the correlogram view of a series for this purpose. This phase of the ARIMA modeling procedure is called identification.

The next step is to decide what kind of ARIMA model to use. If the autocorrelation function dies off smoothly at a geometric rate, and the partial autocorrelations were zero after one lag, then a firstorder autoregressive model is appropriate. Alternatively, if the autocorrelations were zero after one lag and the partial autocorrelations declined geometrically, a first order moving average process would seem appropriate.

#### <sup>102</sup> 6 ii. Estimating ARIMA Models

To specify your ?????????? model, you will difference your dependent variable, if necessary, to account for the order of integration and describe your structural regression model (dependent variables and regressors) and add any ???? ?????????? terms. The d operator can be used to specify differences of series. To specify first differencing, simply include the series name in parentheses after d. For example, ??(?????????????) specifies the first difference of rainfall.

110 Where ?? is the lag operator.

111

(3) c) Basic Concept of Fuzzy Time Series 1994) proposed the definition of fuzzy time series based on fuzzy sets in Zadeh (1965) as follows: Let ?? be the universe of discourse, ?? = {?? 1, ?? 2, ?, ?? ?? } and let ?? be a fuzzy set in the universe of discourse ?? defined as follows:?? = ?? ?? (?? 1) ?? 1 ? + ?? ?? (?? 2) ?? 2 (?? 2) ?? ?? (?? ?) ?? ?? ?? (5)

where ?? ?? is the membership function of ??. ?? ?? ?? ?? [0,1], ?? ?? (?? ??) indicates the grade of membership of ?? ?? in the fuzzy set ??, ?? ?? (?? ??) ? [0,1] and 1 ? ?? ???.

Let ??(??) (?? = ?, 0,1,2, ?) be the universe of discourse and be a subset of ??, and let fuzzy set ?? ?? (??) (?? = 1.2, ?) be defined in ??(??). Let ??(??) be a collection of ?? ?? (??) (?? = 1.2, ?). Then, ??(??) is called a fuzzy time series of ??(??) (?? = ?, 0,1,2, ?).

If ??(??) is caused by ??(?? ? 1), denoted by ??(?? ? 1) ? ??(??), then this relationship can be represented by ??(??) = ??(?? ? 1) ? ??(??, ?? ? 1), where the symbol ?? ? ?? denotes the Max-Min composition operator; ??(??, ?? ? 1) is a fuzzy relation between ??(??) and ??(?? ? 1) and is called the first-order model of ??(??).

Let ??(??) be a fuzzy time series and let ??(??, ??)?

### <sup>125</sup> 7 i. Fuzzy Time Series Model

126 Using the time-variant fuzzy time-series model, the following steps form the procedure.

- 127 Step 1: Define the universe of discourse within which fuzzy sets are defined.
- 128 Step 2: Partition the universe of discourse ?? into several even and equal length intervals.

Step 3: Determine some linguistic values represented by fuzzy sets of the intervals of the universe of discourse.
Step 4: Fuzzify the rainfall data.

Step 5: Choose a suitable parameter  $\eth$  ??" $\eth$  ??", where  $\eth$  ??" $\eth$  ??" > 1, calculate ??  $\eth$  ??" $\eth$  ??" (??, ?? ? 1) and forecast the rainfall as follows:??(??) = ??(?? ? 1) ? ??  $\eth$  ??" $\eth$  ??" (??, ?? ? 1)

where ??(??) denotes the forecasted fuzzy rainfall of year ??, ??(?? ? 1) denotes the fuzzified rainfall of year 134 ?? ? 1, and??  $\eth$  ??" $\eth$  ??" (??, ?? ? 1) = ?? ?? (?? ? 2) × ??(?? ? 1) ? ?? ?? (?? ? 1) × ??(?? ? 2) ? ? ?? ?? 135 (?? ?  $\eth$  ??" $\eth$  ??") × ??(?? ?  $\eth$  ??" $\eth$  ??" + 1)

where  $\eth$  ??" $\eth$  ??" is called the "model basis" denoting the number of years before ??, ?? × ?? is the Cartesian product operator, and ?? is the transpose operator.

138 Step 6: Defuzzify the forecasted fuzzy rainfall using neural nets.

139 It very important to note that we will divide each interval derived in ???????? 2 into four subintervals of equal

- 140 length, where the 0.25-point and 0.75-point of each interval are used as the upward and downward forecasting 141 points of the forecasting. Three rules were used and they are:
- interval corresponding to the fuzzified rainfall ?? ?? with the membership value equal to 1.

### <sup>143</sup> 8 If (|the difference of the differences between years

n-1 and n-2 and between years n-2 and n-3/2? the rainfall data of year n-1) or (the rainfall data of year n-1-|the 144 difference of the differences between years n-1 and n-2 and between years n-2 and n-3/2 falls in the interval of 145 the corresponding fuzzified rainfall ?? ?? with the membership value equal to 1, then the trend of the forecasting 146 of this interval will be downward, and the forecasting rainfall falls at the 0.25-point of the interval corresponding 147 to the fuzzified rainfall ?? ?? with the membership value equal to 1; if (|the difference of the differences between 148 years n-1 and n-2 and between years n-2 and  $n-3 \times 2$ ? the rainfall data of year n-1) or (the rainfall data of year 149 n-1 -|the difference of the differences between years n-1 and n-2 and between years n-2 and n-3|  $\times$  2) falls in the 150 interval corresponding to the fuzzified rainfall ?? ?? with the membership value equal to 1, then the trend of 151 the forecasting of this interval will be upward, and the forecasting rainfall falls at the 0.75-point of the interval 152 corresponding to the fuzzified rainfall with the membership value equal to 1; if neither is the case, then we let 153 the forecasting rainfall be the middle value of the interval corresponding to the fuzzified rainfall ?? ?? with the 154 membership value equal to 1. 155

### <sup>156</sup> 9 d) Theil's Regression

### <sup>164</sup> **10 f**) Data

The annual rainfall of Ibadan in South West region of Nigeria which is bounded by 3 0 53 ? , 7 0 22 ? will be used for this study. The data was obtained from the Nigerian Meteorological Agency, Lagos. It consists of the annual rainfall from 1981 to 2012 (31 years). The universe of discourse [600, 1800] is redivided into the following intervals:

# <sup>169</sup> 11 Fuzzy Time Series Steps

# 170 12 Results and Discussion

171 It is evidence from the time plots that rainfall data displays series of cyclical behaviour and this is due to seasonal 172 changes yearly. For autoregressive integrated moving average, model building commenced with the examination 173 of the plot of the series, the sample plot of the autocorrelation (ACF) and partial autocorrelation (PACF) model 174 description. The time plot of the original series (??????. 1) shows stationarity as confirmed by the Augmented 175 Dickey-fuller test in (Table 1) with a p-value of 0.05, but with seasonal trend.

Since the order of integration of the differenced rainfall series in (fig. ??) is two, then ?? = 2 ?????? a close look of the ACF and PACF of the differenced data in (fig. ??) revealed the ACF dies off smoothly at a geometric rate and the partial autocorrelations were zero after one lag and the autocorrelations were zero after one lag and the partial autocorrelations declined geometrically, these behaviour shows that ?????????? (1,2,1) is the appropriate model for the differenced rainfall series, that is (1 ? ?? 1 ??)? 2 ?? ?? = (1 ? ????)?? ?? .Thereforethe fitted model is given as:?? ?? = 4.37 + ?? ?? (1 ? 0.39??)?? ?? = (1 ? 0.99??)?? ??

With the white noise variance ?? ?? 2 estimated as 17452. In order to use the model obtained for forecast some model diagnostic test were carried out. The inverse root of ???????? in (fig. 3) shows that the estimated ARMA process is (covariance) stationary, since all AR roots lie inside the unit circle and the estimated ARMA process is invertible, since all MA roots should lie inside the unit circle. The correlogram has no significant spike and all subsequent Q-statistics are not highly significant. This result clearly indicates there is no need for respecification of the model. However, the forecast of the yearly rainfall from 1982 to 2012 deviated slightly from the original data, ?????? ??????. (5).

<sup>189</sup> Under fuzzy time series, we made use of the visual Basic Version 6.0 on a Pentium 4 PC. Tab. 4 summarizes <sup>190</sup> the forecasting results of fuzzy time series method from 1982 to 2012, where the universe of discourse is divided <sup>191</sup> into 13 intervals and the interval with the largest number of rainfall data is divided into 4 sub-intervals of equal <sup>192</sup> length. The fuzzy time series forecast of the yearly rainfall data from 1982 to 2012 did not deviated much from <sup>193</sup> the original data, ?????? ??????. (4) ?????? ??????. (5).

Using the non-parametric method (theil's regression), we obtain a fitted linear model: ?? = 900.98 + 10.12(??), where ?? represents rainfall data and ?? represents time.

# <sup>196</sup> 13 a) A Comparison of Different Forecasting Methods

The performance measures of ARIMA, FTS and theil's regression models in terms of numerical computations are shown in 226.12 respectively. While the same MAE is considerably lower at 85.45 for FTS model. The other performance measures such as RMSE and ?? 2 depict that the FTS forecast is superior to ARIMA and theil's regression forecast. The forecast graph in fig. 5 as well shows clearly that FTS forecast did not deviate much from the original data compared to the two other models. Therefore, our study establishes that FST method should be favoured as an appropriate forecasting tool to model and predict annual rainfall.

# <sup>203</sup> 14 V. Conclusion

Complexity of the nature of annual rainfall record has been studied using FST, ARIMA and Theil's regression techniques. An annual rainfall data spanning over a period of 1982 -2012 of Ibadan in South West, Nigeria was used to develop and test the models. The study reveals that FST model can be used as an appropriate forecasting

207 tool to predict the rainfall, which out performs the ARIMA and Theil's regression model.

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Figure 1: Statistical



Figure 2: 1 .



Figure 3: Figure 3:



Figure 4: Figure 2 : Figure 1 :

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[Note: 1, ?? 1), (?? 2, ?? 2), ?, (?? ??, ?? ?? ) are described by the equation; ?? = ?? + ????. The calculation of ?? and ?? follows the steps outlined below;? All ?? data points are ranked in ascending order of ?? values. ?]

Figure 5:

1						
t-Statistic		Prob.*				
[Note: Figure 3 : Inverse Root of ARMA]						
Figure 6: Table 1 :						
2						
Number of		1	3 11	10 4 2		
Tannan Gava						
Figure 7: Table 2 :						
3						
Year Rainfall Trend of the Forecasting Forecasting						
	Year 2014 DDDDDDDD)G					
		(				
Figure 8: Table 3 :						
4						
Model A RIM A	MAE 110-23	RMSE	????			
Fuzzy Time	85.45	9.24	0.97882			
Series	006.10	15.00	0.00040			
Theil's Regression IV.	226.12	15.03	0.83346			
Figure 0. Table 4.						

4

Figure 10: Table 4 .

### 14 V. CONCLUSION

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